

2. Determination of mass & mixing

Two effects

Solar
neutrinos

KamLAND

Atmospheric
neutrinos

Double Chooz

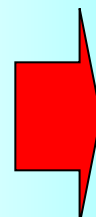
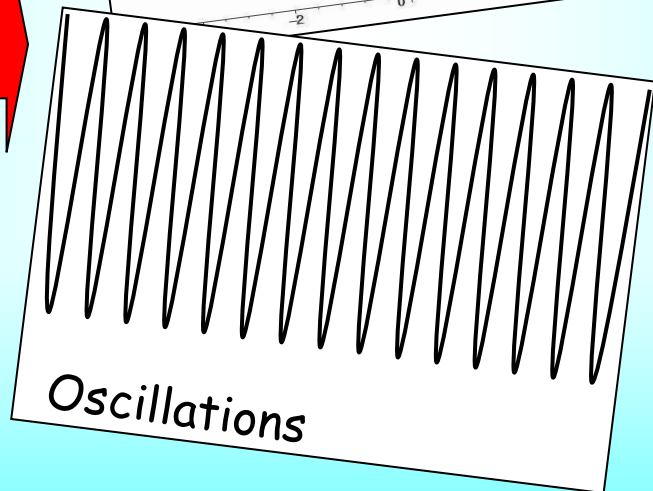
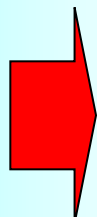
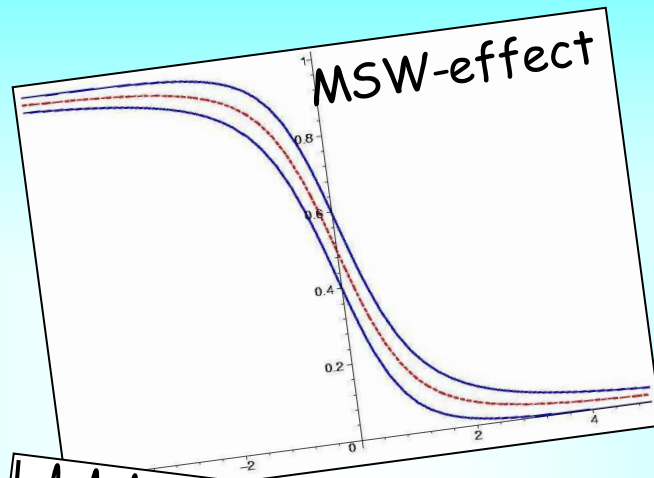
Daya Bay

MINOS

K2K RENO

T2K Antares

DeepCore

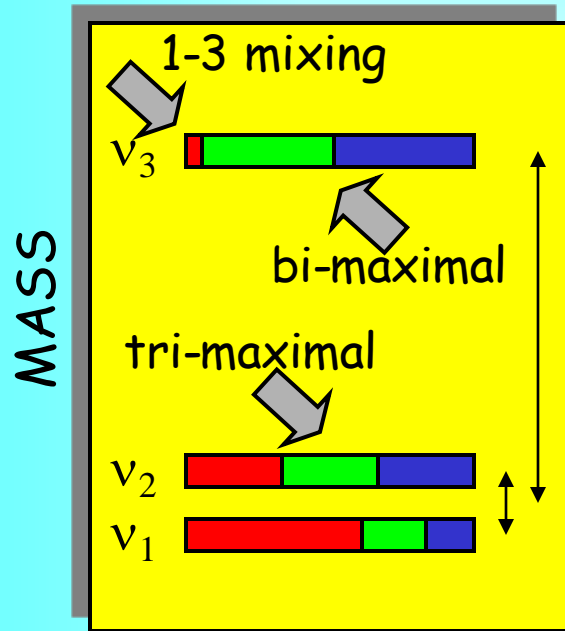
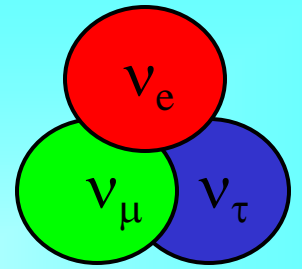


$$\Delta m^2$$
$$\theta$$

Can be resonantly
enhanced in matter

			Dominant mode	
Solar neutrinos KamLAND	$\nu_e - \nu_e$		MSW-effect (HE) Av. oscillations (LE)	1 - 2
	$\nu_e - \nu_e$		Vacuum oscillations	1 - 2
Atmospheric neutrinos SK	$\nu_\mu - \nu_\mu$	$\nu_\mu - \nu_\tau$	~ Vacuum oscillations	1 - 3
	$\nu_\mu - \nu_\mu$			
Antares Deepcore	$\nu_\mu - \nu_\mu$			
	$\nu_\mu - \nu_\mu$	$\nu_\mu - \nu_e$	~ Vacuum oscillations	1 - 3
MINOS K2K	$\nu_\mu - \nu_\mu$			
	$\nu_\mu - \nu_\mu$			
Double Chooz Dava Bay RENO	$\nu_e - \nu_e$		Vacuum oscillations	1 - 3
	$\nu_\mu - \nu_e$	$\nu_\mu - \nu_\mu$	~ Vacuum oscillations	1 - 3
T2K	$\nu_\mu - \nu_e$	$\nu_\mu - \nu_\mu$	~ Vacuum oscillations	1 - 3

Mixing & masses



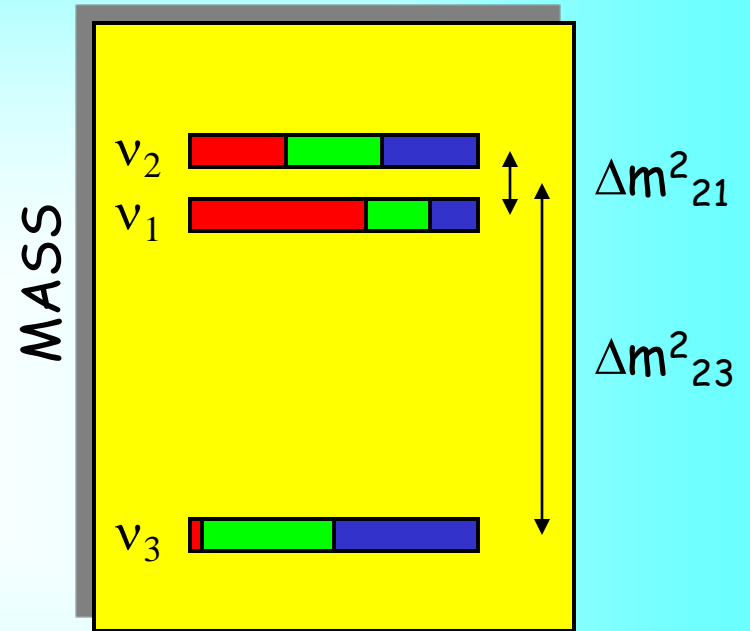
FLAVOR

Normal mass hierarchy

$$\Delta m^2_{32}$$

$$\Delta m^2_{21}$$

?



FLAVOR

Inverted mass hierarchy

$$\Delta m^2_{21}$$

$$\Delta m^2_{23}$$

Two large mixings

~ Tri-bimaximal mixing

$$\Delta m^2_{32} = 2.3 \times 10^{-3} \text{ eV}^2$$

$$\Delta m^2_{21} = 8 \times 10^{-5} \text{ eV}^2$$

Symmetry?

$\nu_\mu - \nu_\tau$ symmetry

Invariance under U, S transformations in the flavor basis

Tri-bimaximal mixing

L. Wolfenstein

In the first approximation

$$U_{\text{tbm}} = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

0.15

0.62

0.78



ν_3 is bi-maximally mixed
 ν_2 is tri-maximally mixed

*P. F. Harrison
 D. H. Perkins
 W. G. Scott*

- maximal 2-3 mixing
- zero 1-3 mixing
- no CP-violation

- $\sin^2\theta_{12} = 1/3$

$U_{\text{tbm}} = U_{23}(\pi/4) U_{12}$

Uncertainty related to sign of 2-3 mixing:
 $\theta_{23} = \pi/4 \rightarrow -\pi/4$

Symmetry from mixing matrix

Huge impact of small angle

theoretical
implications

symmetry

atmospheric
neutrinos

θ_{e3}

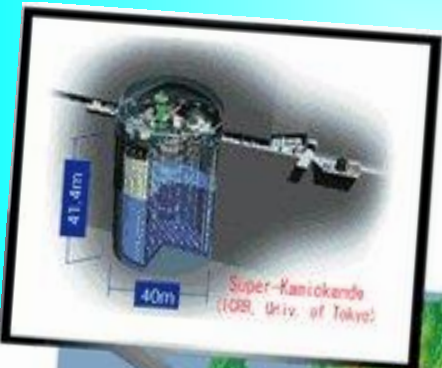
dominant factor
for SN neutrinos

door to determination of
CP-violation
mass hierarchy

Discovering ν_{e3}

MINOS

Global fit
Solar vs KamLAND



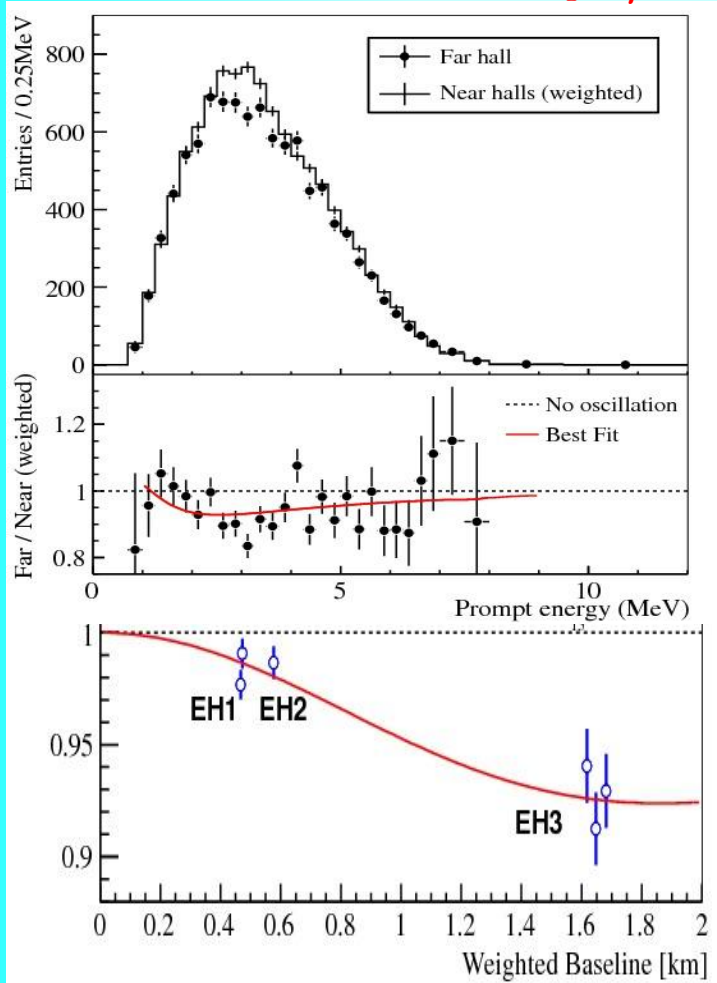
T2K



Double-CHOOZ

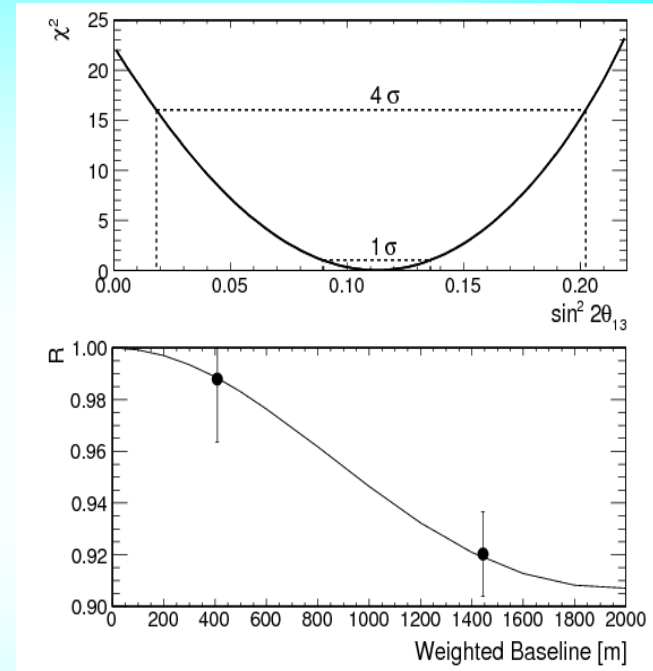
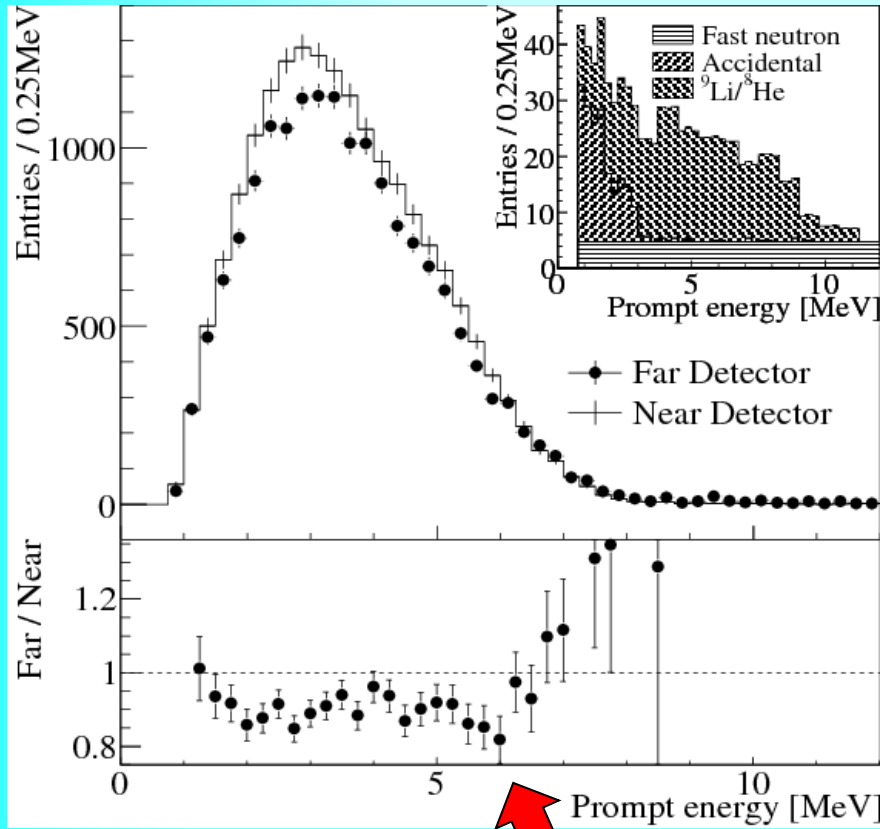
Daya Bay

arXiv:1203.1669 [hep-ex]

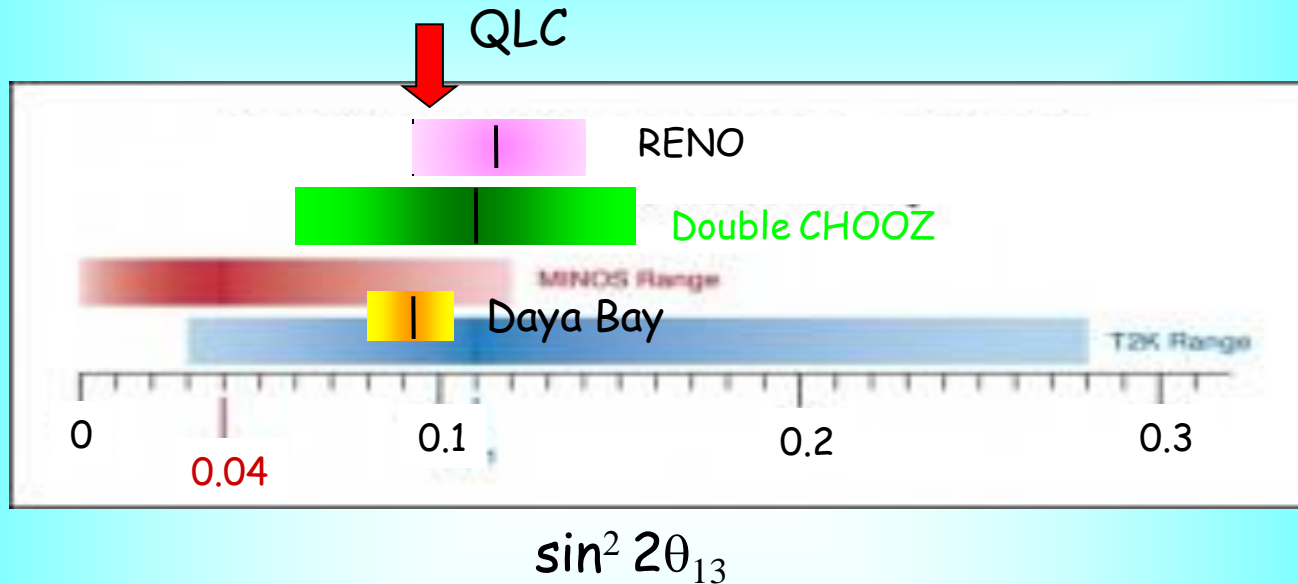


$W = 2.9 \text{ GW}$ (each of 6 reactor)
AD (antineutrino detectors)
EH (experimental halls)

RENO



Direct measurements of θ_{13} mixing



Daya Bay: 0.092 ± 0.012

RENO: 0.116 ± 0.024

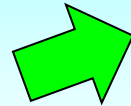
$> 6\sigma$ from 0

Important: Daya Bay, RENO and T2K
(different energies, setups..) give the same value of the angle

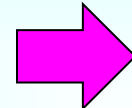
Deviation of 2-3 mixing from maximal

$$d_{23} = \frac{1}{2} - \sin^2 \theta_{23}$$

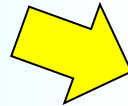
the key to (probe)
understand the
underlying physics



$\nu_\mu - \nu_\tau$ symmetry
violation

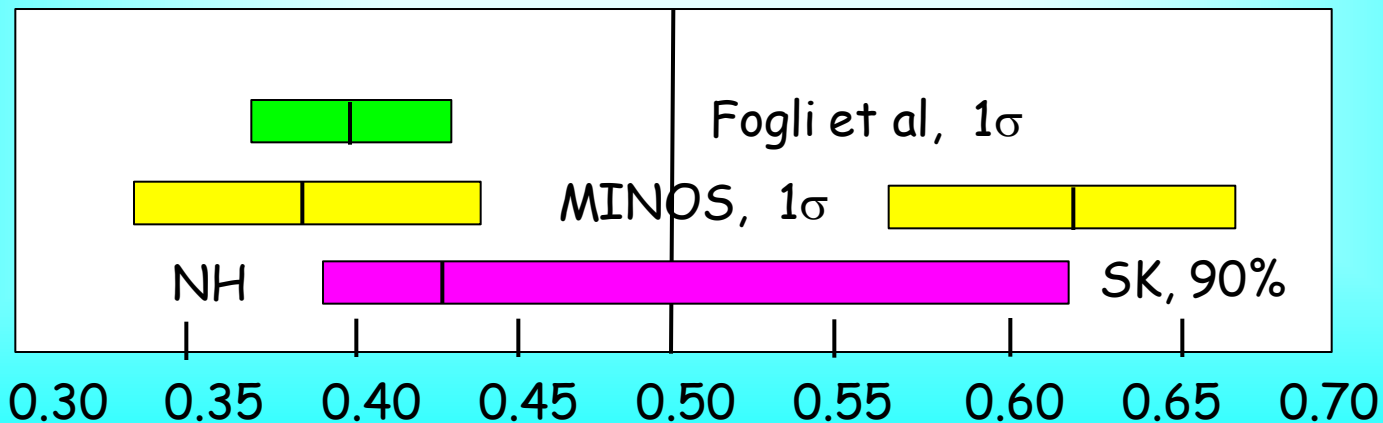


Connection to
1-3 mixing



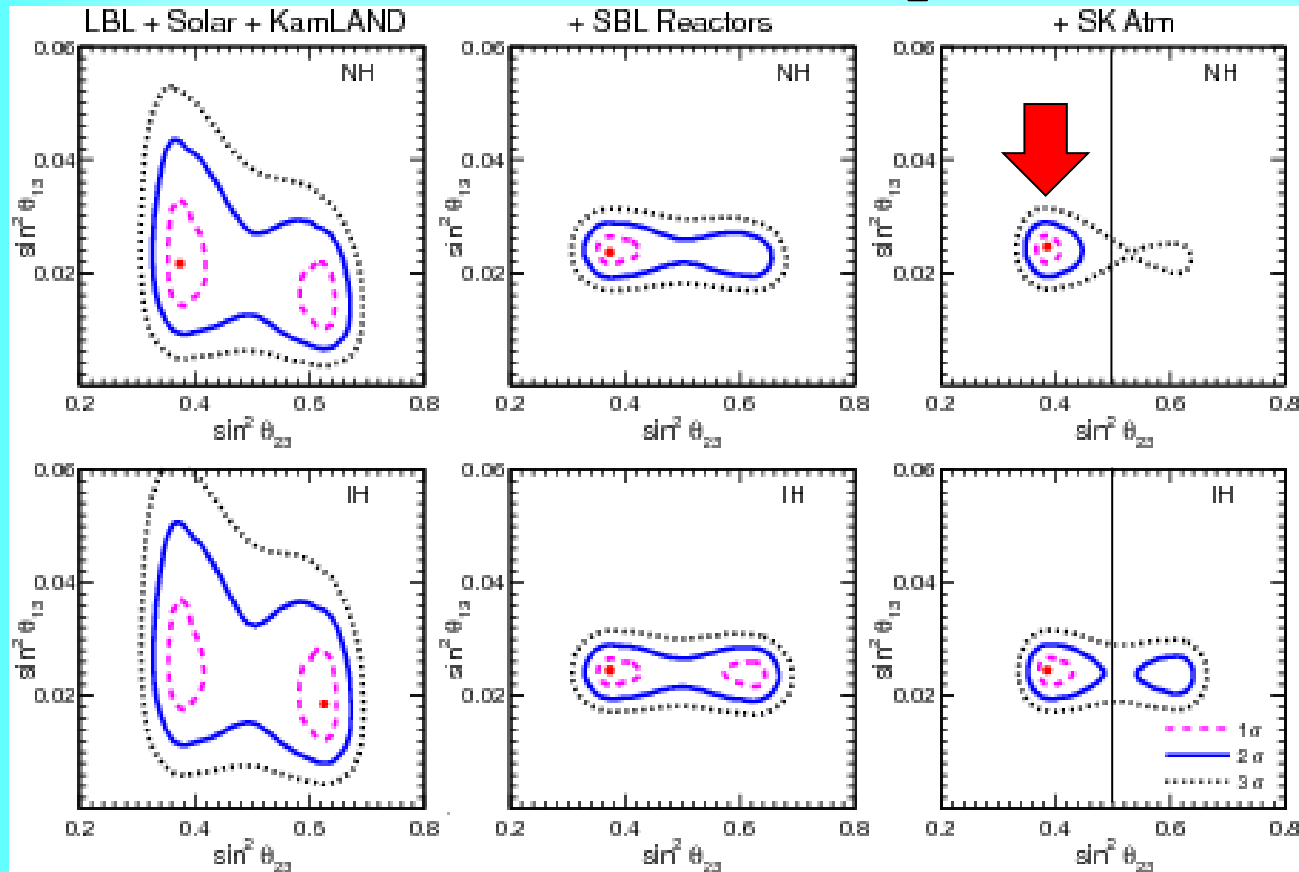
Quark -Lepton
Complementarity

$$\theta_{23} \sim \pi/2 - V_{cb}$$



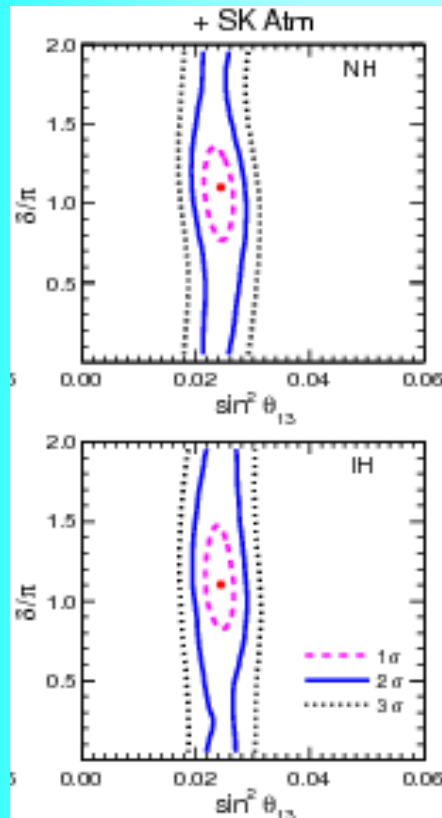
$\sin^2 \theta_{23}$

2-3 deviation and quadrant



Global fit of oscillation data

CP-phase: measurements and predictions



G. L. Fogli

First glimpses?

T. Yanagida $\delta_{CP} \sim \pi/2 \pm 0.02$

Neutrino-antineutrino asymmetry

Dependence of probabilities on energy in wide range

Reconstruction of unitarity triangle

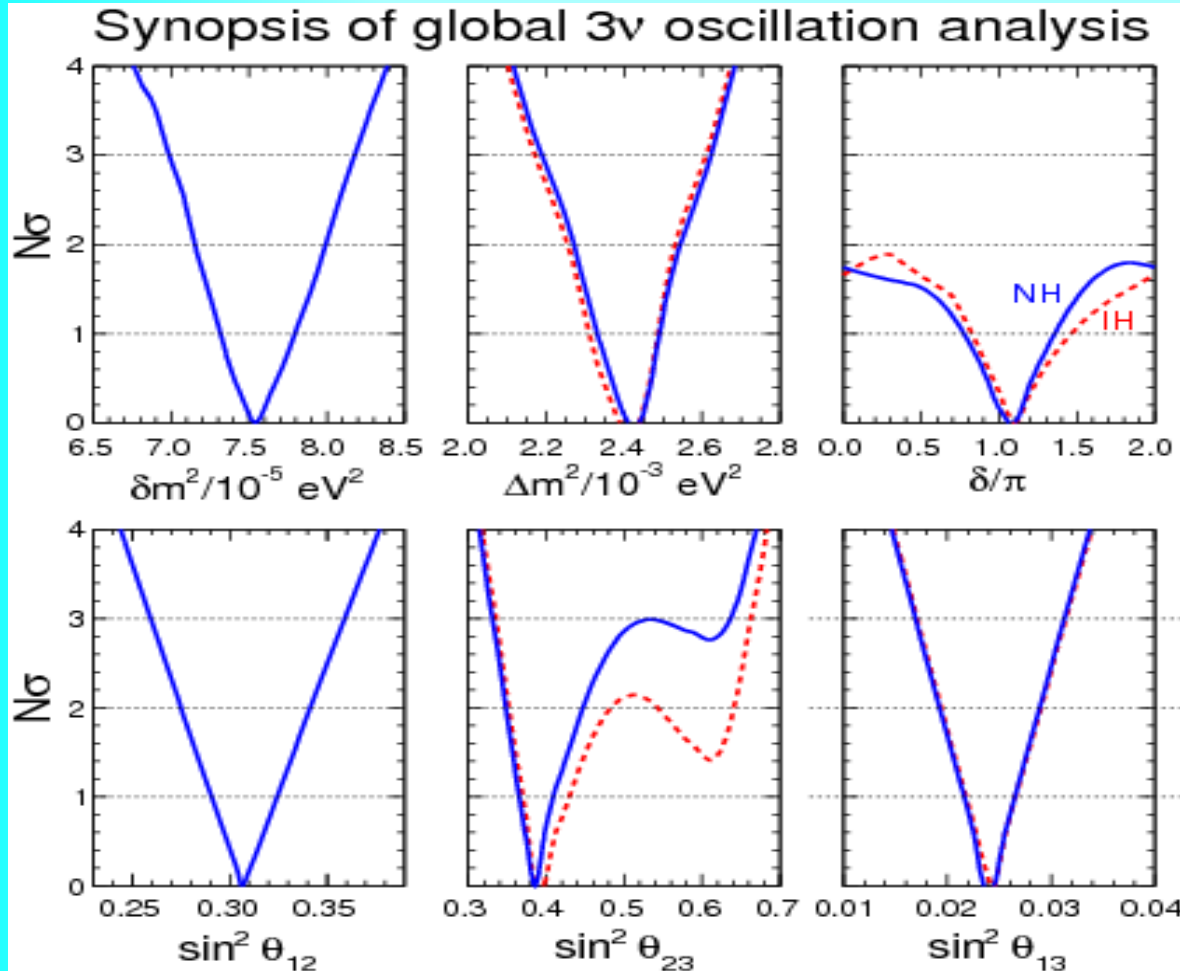
Key measurement: amplitudes of the $\nu_\mu - \bar{\nu}_\mu$ oscillations due to solar and atmospheric mass splittings

Third way

Do we have predictions for the phase in quark sector?
 Why do we think that we can predict leptonic mixing?
 Again because of neutrinos are special? Symmetries?

Synopsis

G. L. Fogli



Serious implications
for theory

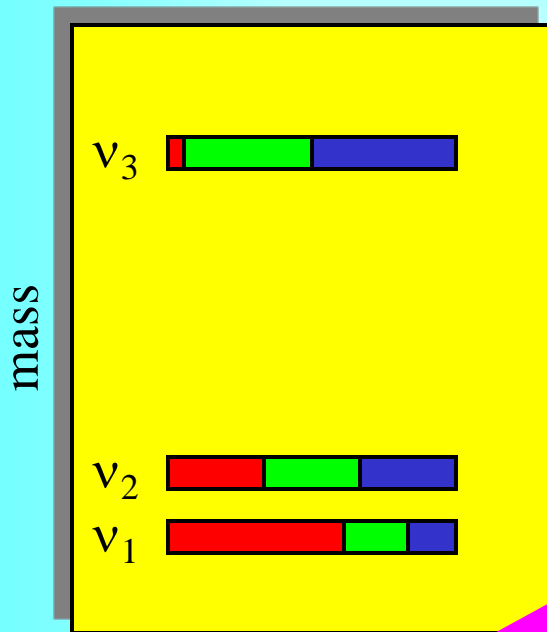
Non-zero, relatively
Large 1-3 mixing

Substantial deviation
of the 2-3 mixing
from maximal

$$\delta_{CP} \sim \pi$$

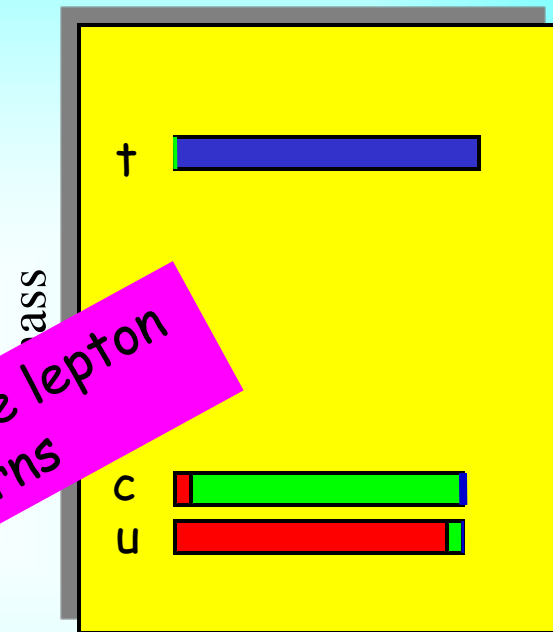
Robust ?

Leptons versus quarks



Leptons

$$\nu_f = U_{\text{PMNS}} \nu_{\text{mass}}$$



Quarks

$$U_d = U_{\text{CKM}}^\dagger U$$

Strong difference of the lepton and quark mixing patterns

$$U = (u, c, t)$$

combination of down-quarks produced with a given up quark

Mass scale



Oscillations,
& cosmology



the heaviest neutrino has
mass is in the range
(0.045 - 0.10) eV

Oscillations:

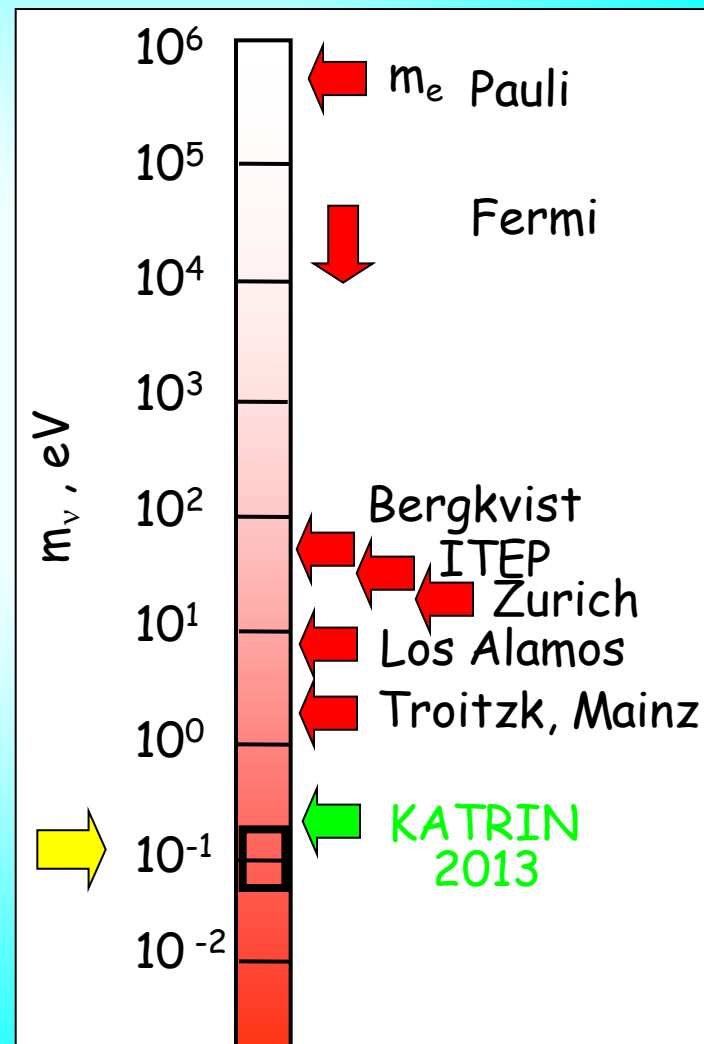
$$\frac{m_2}{m_3} \gtrsim 0.18$$

\gtrsim

0.18

the weakest
mass hierarchy

Kinematical methods



Cosmological bounds

Λ CDM

- WMAP 7yr
- SDSS III 8th data release
- Hubble space telescope H

*R. De Putter et al,
arXiv: 1201.1909
[astro-ph.CO]*

$$\Sigma m < 0.26 \text{ eV (95 \% CL)}$$

Conservative bias

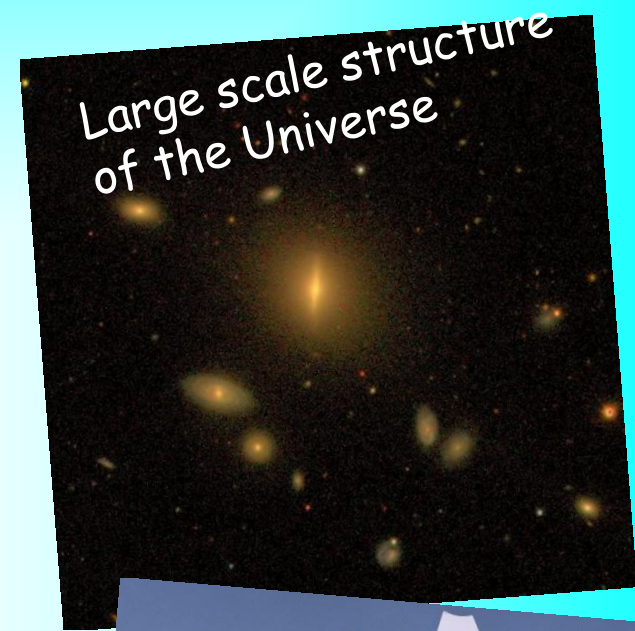
$$\Sigma m < 0.36 \text{ eV (95 \% CL)}$$

- WMAP 7yr
- Observable Hubble
parameter data (OHD)
- H_0 (in correlation with σ_8)

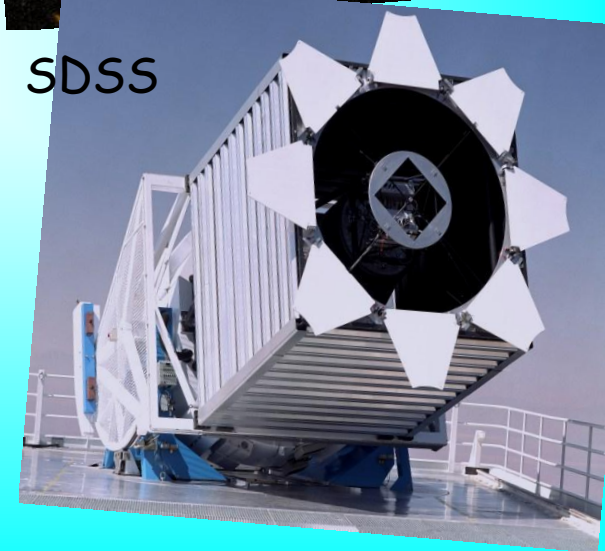
*M. Moresco, et al.,
arXiv:1201.6658
[astro-ph.CO]*

$$\Sigma m < 0.24 \text{ eV (68 \% CL)}$$

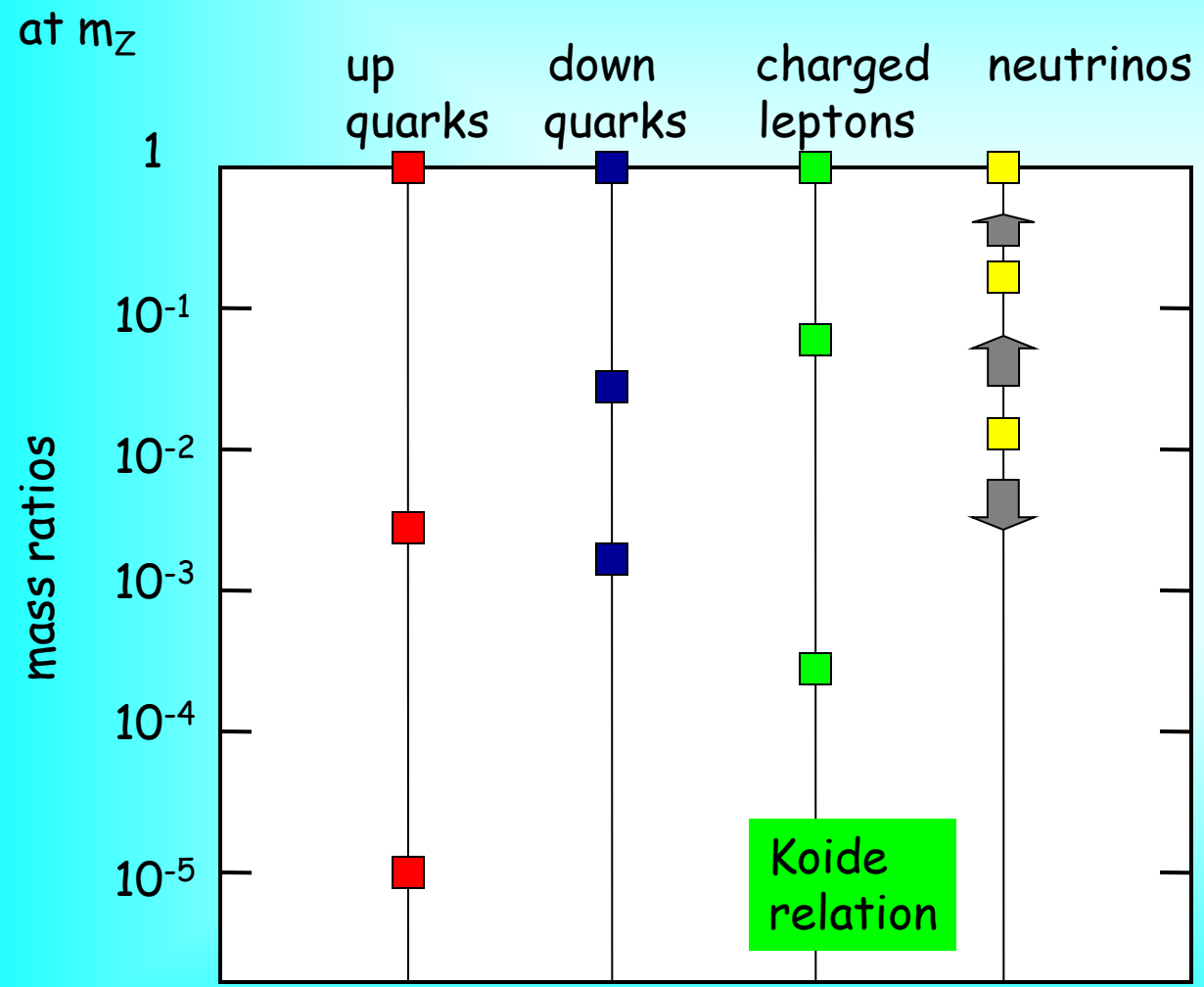
Future: $\Sigma m < 0.08 \text{ eV}$



SDSS



Mass hierarchies



Solar, KamLAND

$$\frac{m_2}{m_3} \geq \sqrt{\frac{\Delta m_{21}^2}{\Delta m_{32}^2}}$$

~ 0.18

Neutrinos have the weakest mass hierarchy (if any) among fermions

Related to the large lepton mixing?

$$m_u m_t = m_c^2$$

$$\sin\theta_C \sim \sqrt{m_d/m_s}$$

Gatto-Sartori-Tonin relation

Double beta decay

$$m_{ee} = U_{e1}^2 m_1 + U_{e2}^2 m_2 e^{i\alpha} + U_{e3}^2 m_3 e^{i\beta}$$

In terms of the lightest mass eigenstate

$$m_{ee} = U_{e1}^2 m_1 + U_{e2}^2 (\Delta m_{21}^2 + m_1^2)^{1/2} e^{i\alpha} + U_{e3}^2 (\Delta m_{31}^2 + m_1^2)^{1/2} e^{i\beta}$$

Normal mass hierarchy

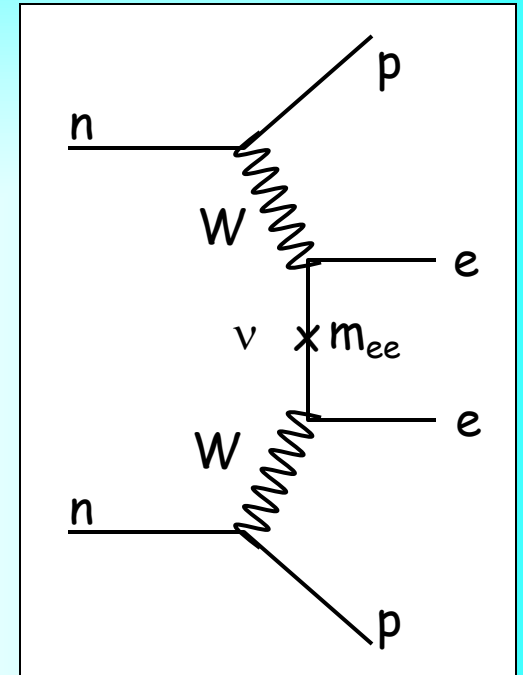
$$m_{ee} = U_{e1}^2 (\Delta m_{13}^2 + m_3^2)^{1/2} + U_{e2}^2 (\Delta m_{23}^2 + m_3^2)^{1/2} e^{i\alpha} + U_{e3}^2 m_3 e^{i\beta}$$

Inverted mass hierarchy

Strong mass hierarchy:

$$m_{ee} \sim U_{e2}^2 (\Delta m_{21}^2)^{1/2} + U_{e3}^2 (\Delta m_{31}^2)^{1/2} e^{i\xi}$$

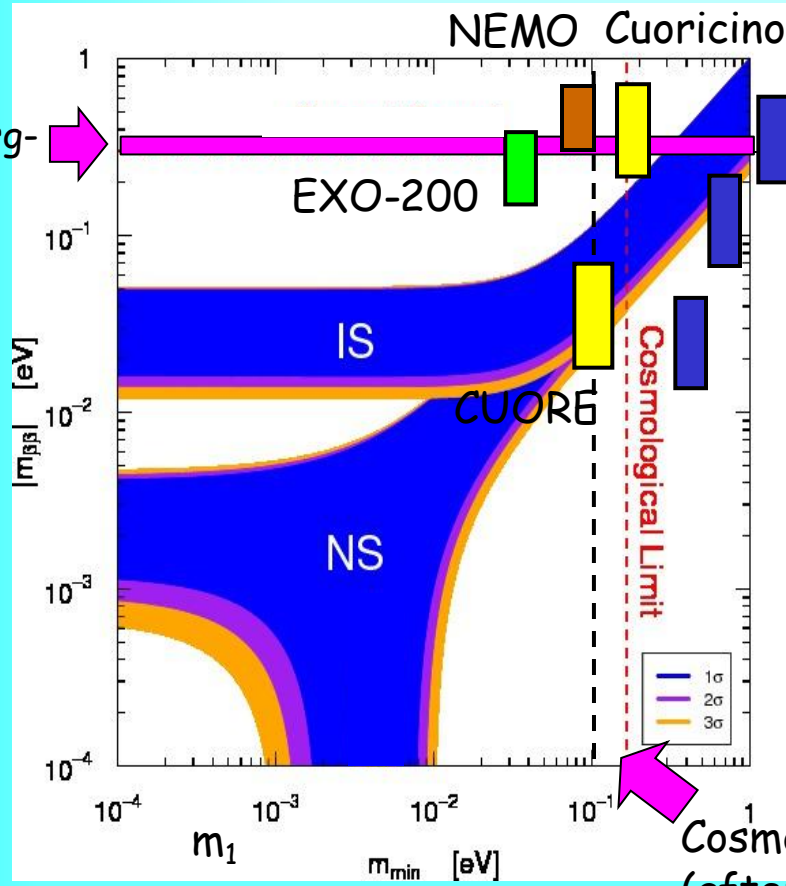
$$m_{ee} \sim (\Delta m_{31}^2)^{1/2} [r c_{13}^2 s_{12}^2 + s_{13}^2 e^{i\xi}]$$



$$m_{ee} = \sum_k U_{ek}^2 m_k e^{i\phi(k)}$$

Sensitivity to the Majorana mass

S M Bilenky C Giunti
arXiv:1203.5250 [hep-ph]



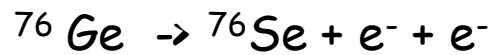
Upper bounds, boxes -
 uncertainties of NME

H-M: $m_{ee} = (0.29 - 0.35) \text{ eV}$

EXO-200: $m_{ee} < (0.14 - 0.38) \text{ eV}$

Cosmology
 (after WMAP-7)

H-M result



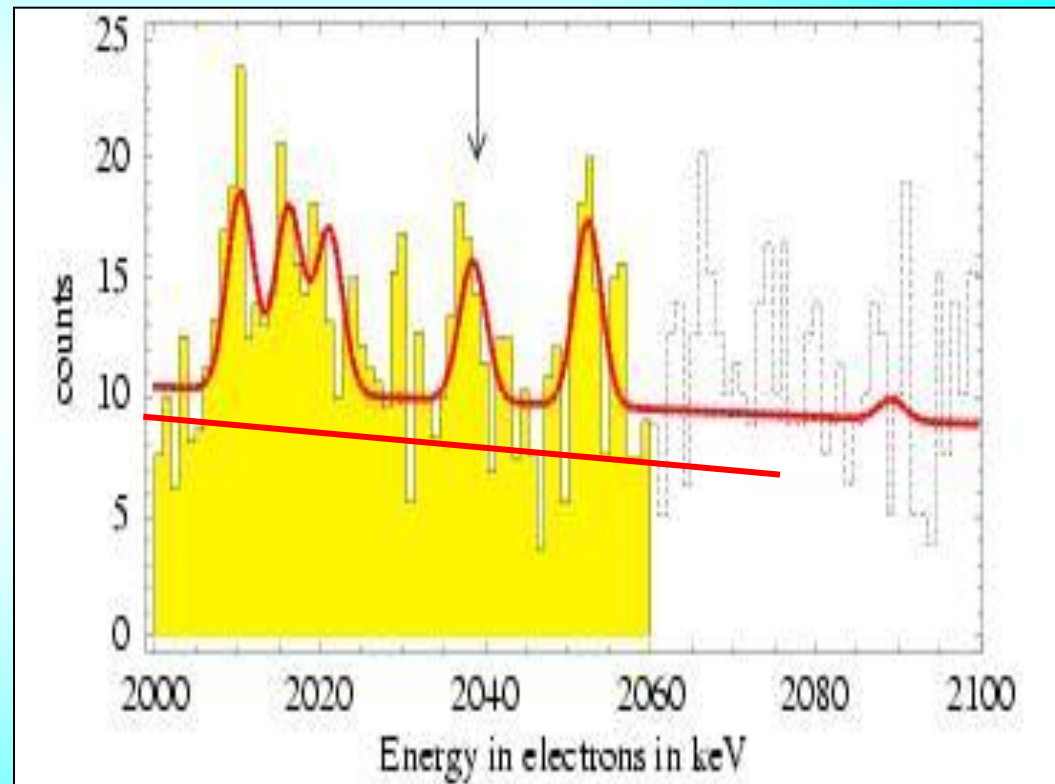
$$T_{1/2} = 2.23^{+0.44}_{-0.31} \times 10^{25} \text{ y} \quad (1\sigma)$$

> 6σ evidence for the observation of $0\nu\beta\beta$ - decay

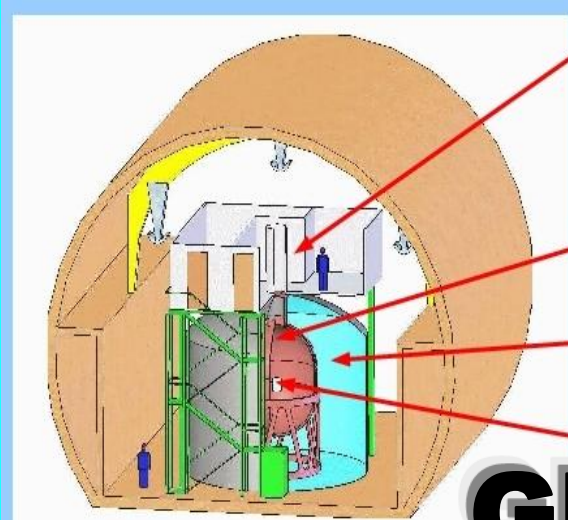
*H. V. Klapdor-Kleingrothaus and
I. V. Krivosheina,
Mod. Phys. Lett. A 21 1547 (2006)*

$$m_{ee} = (0.32 \pm 0.03) \text{ eV}$$

Spectrum near the end point



New experiments



GERmanium
Detector
Array
in LAr

Cryostat

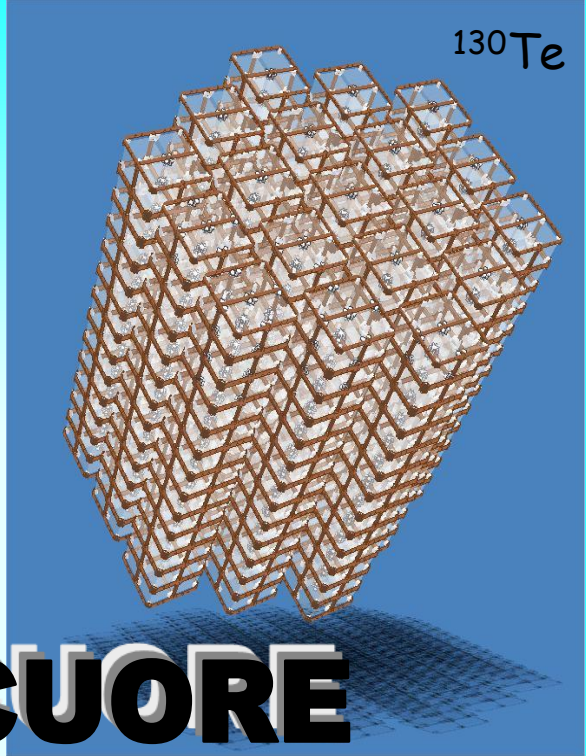
Watertank

Ge detector

GERDA

- Phase I: 15 kg y: 0.3 - 0.9 eV
- Phase II: 37.5 kg y: 0.09 - 0.29 eV
- Phase III: 1 ton 0.01 eV

Xe- Observatory



CUORE

Cryogenic Underground
Observatory for Rare Events



EXO-200

Challenges:

Accomplish reconstruction of neutrino mixing and mass spectrum

Mass hierarchy

CP-violation

Deviation of 2-3 mixing from maximal

Precision measurements of mixing angles

Absolute mass scale

Nature of neutrino mass

Searches for new neutrino states

Now after establishing relatively large 1-3 mixing can be easy

Dirac vs Majorana

3. Race for hierarchy and CP

Mass ordering

$$\Delta m^2_{31} \rightarrow - \Delta m^2_{31}$$

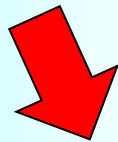
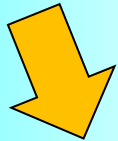
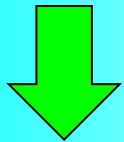
Resonance in the antineutrino
channel $V \rightarrow -V$

Task for everybody:

- * Theory - make predictions
- * Phenomenology - find effects which depend on mass hierarchy and CP-phases
- * Experiment - measure these effects

Race for hierarchy

Matter effect
on 1-3 mixing



Precise
measurements
of Δm^2
at reactors

Cosmology
 Σm

Atmospheric
neutrinos

LBL
experiments

Supernova
neutrinos

Double beta
decay m_{ee}

PINGU

NH \leftrightarrow IH
nu \leftrightarrow antinu

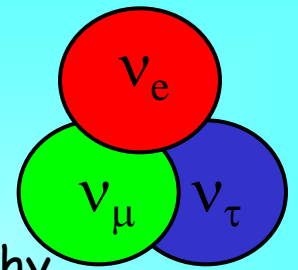
INO

NOvA
Neutrino beam
Fermilab-PINGU(W. Winter)

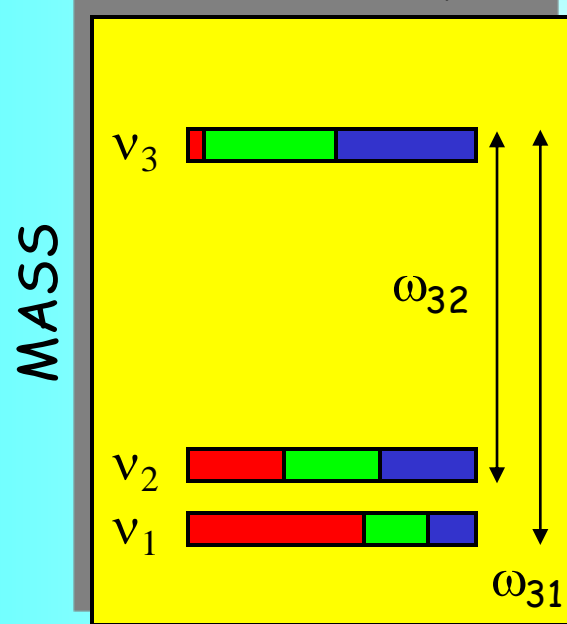
Earth matter
effect
Energy spectrs

Sterile neutrinos
may help?

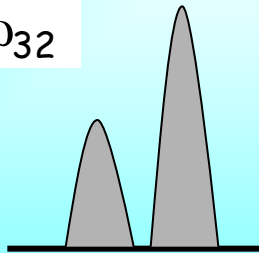
Mass hierarchy (ordering)



Normal hierarchy



$$\omega_{31} > \omega_{32}$$



Oscillations

$$D_{31} \sim 2D_{32}$$

Matter effect

makes the e-flavor heavier →
changes two spectra differently

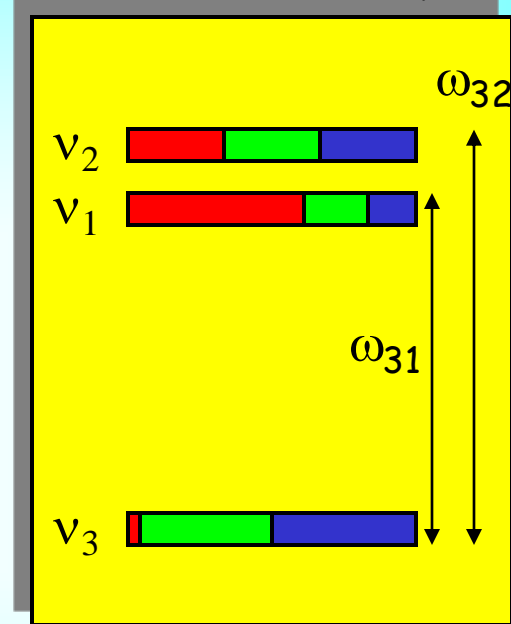
Cosmology

$\beta\beta$ -decay

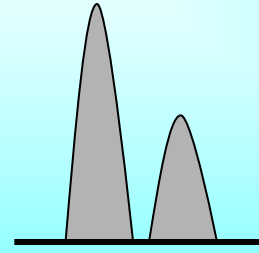
$$\omega_{ij} = \Delta m^2_{ij} / 2E$$

Mass states can be marked by ν_e - admixtures

Inverted hierarchy



$$\omega_{31} < \omega_{32}$$



ω

S. Petcov
M. Piai

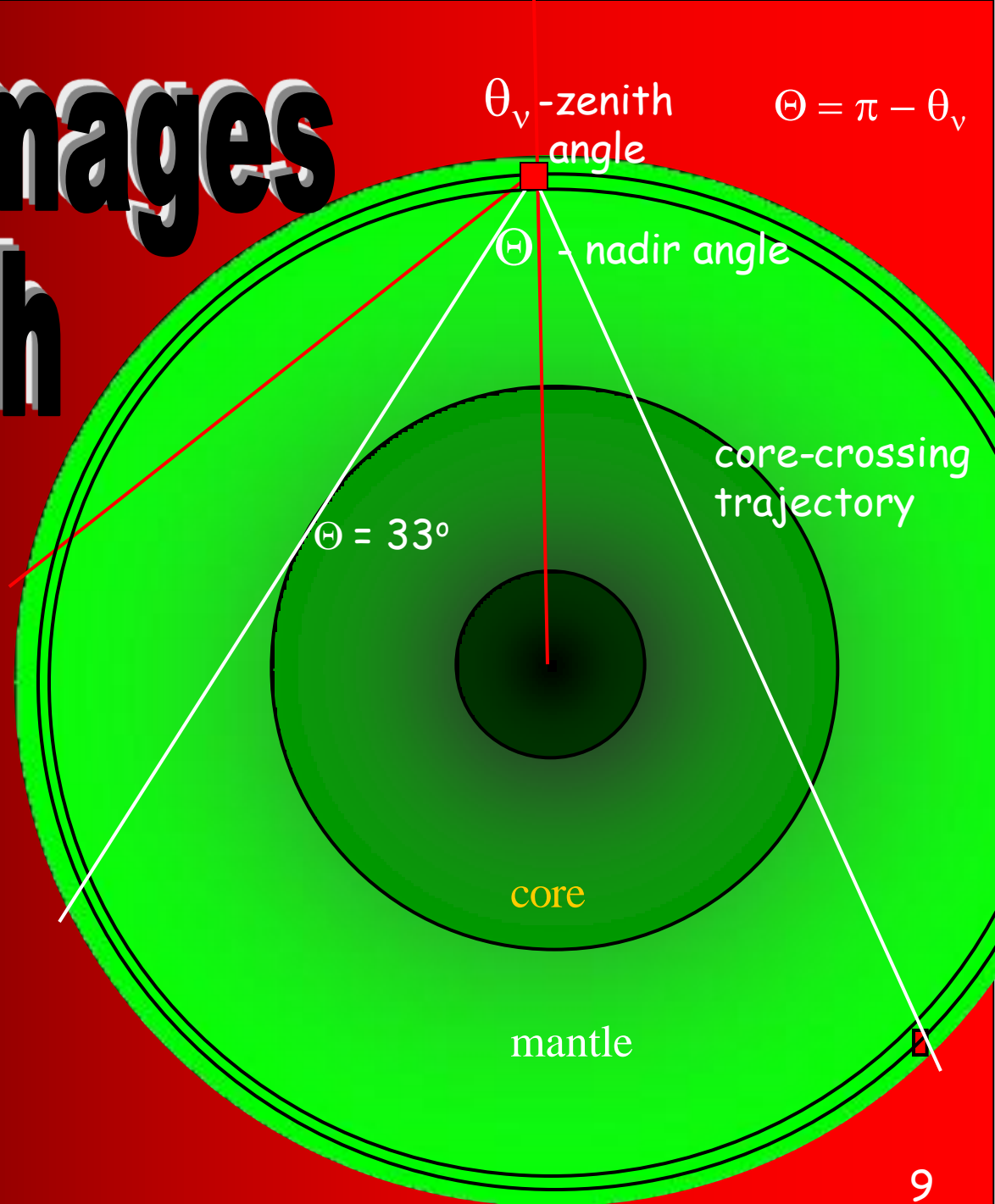
Neutrino images of the Earth

Oscillations in
multilayer medium

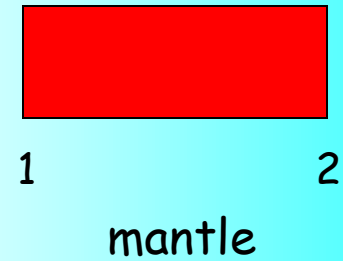
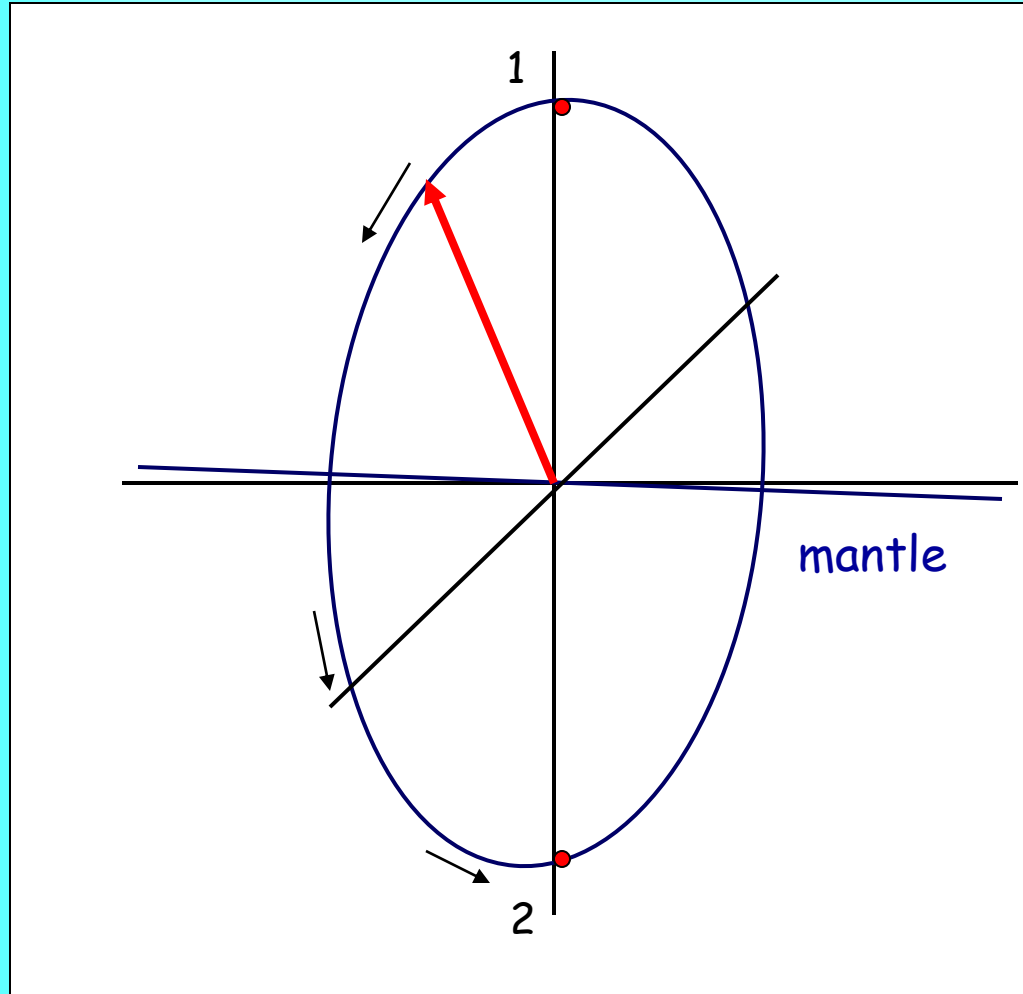
Applications:

flavor-to-flavor transitions

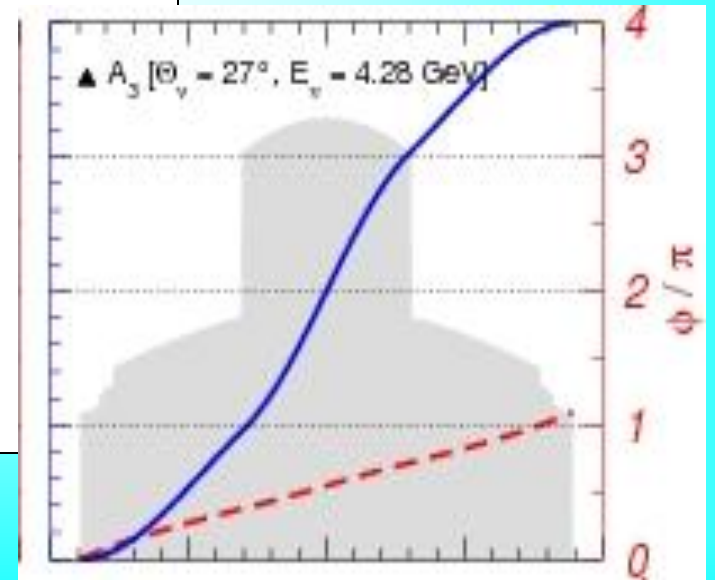
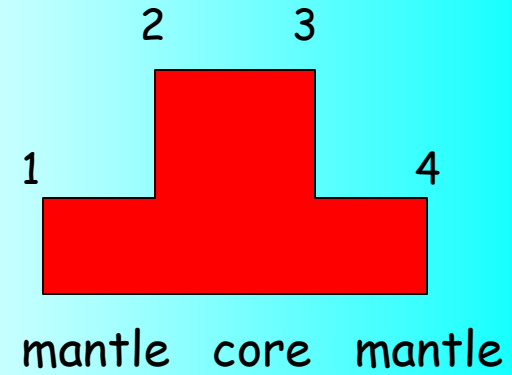
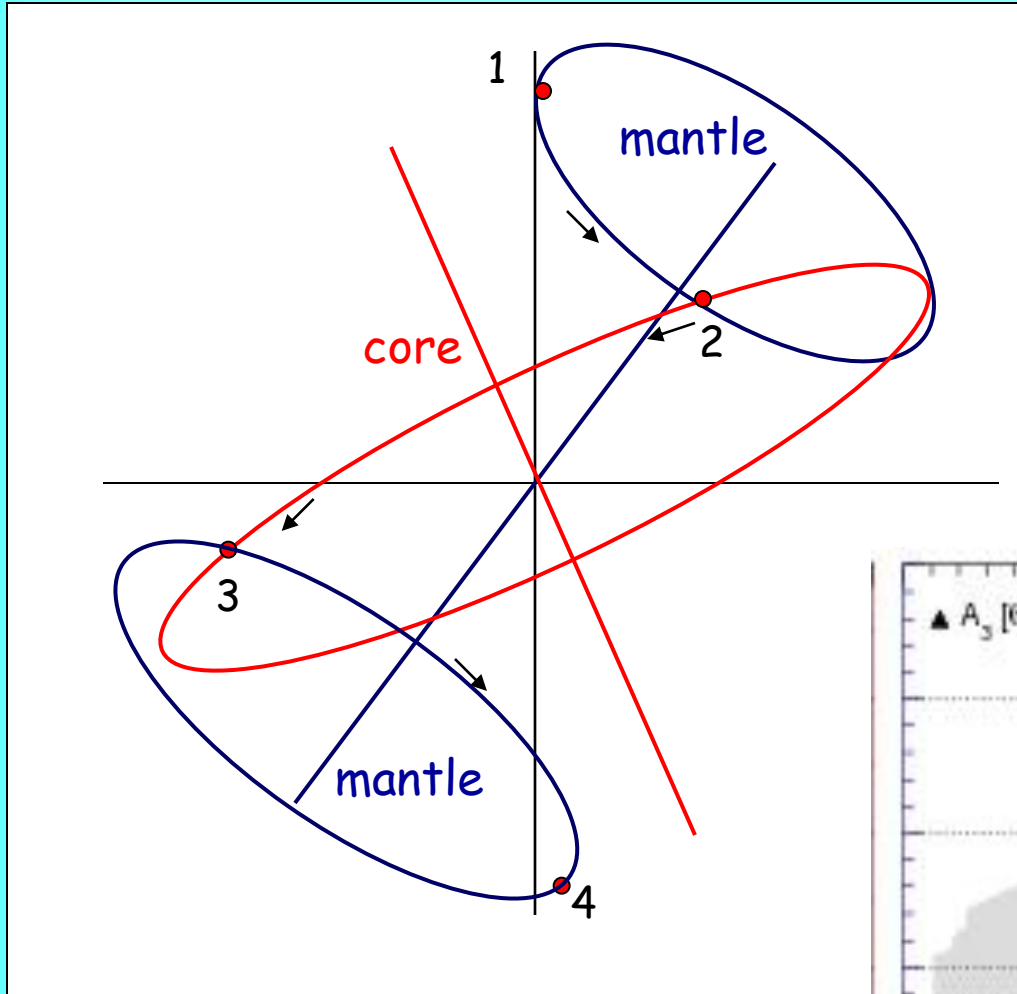
- accelerator
- atmospheric
- cosmic neutrinos



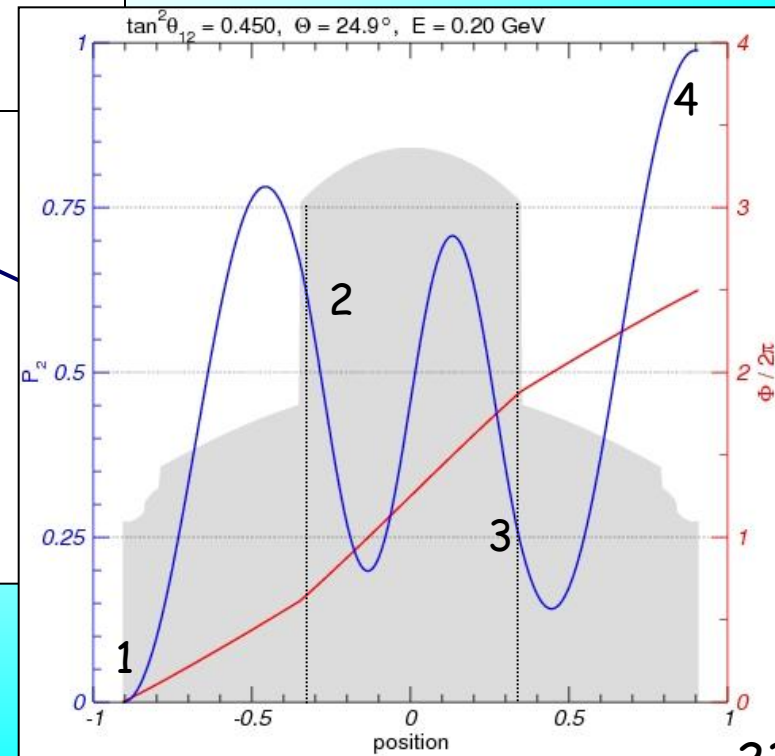
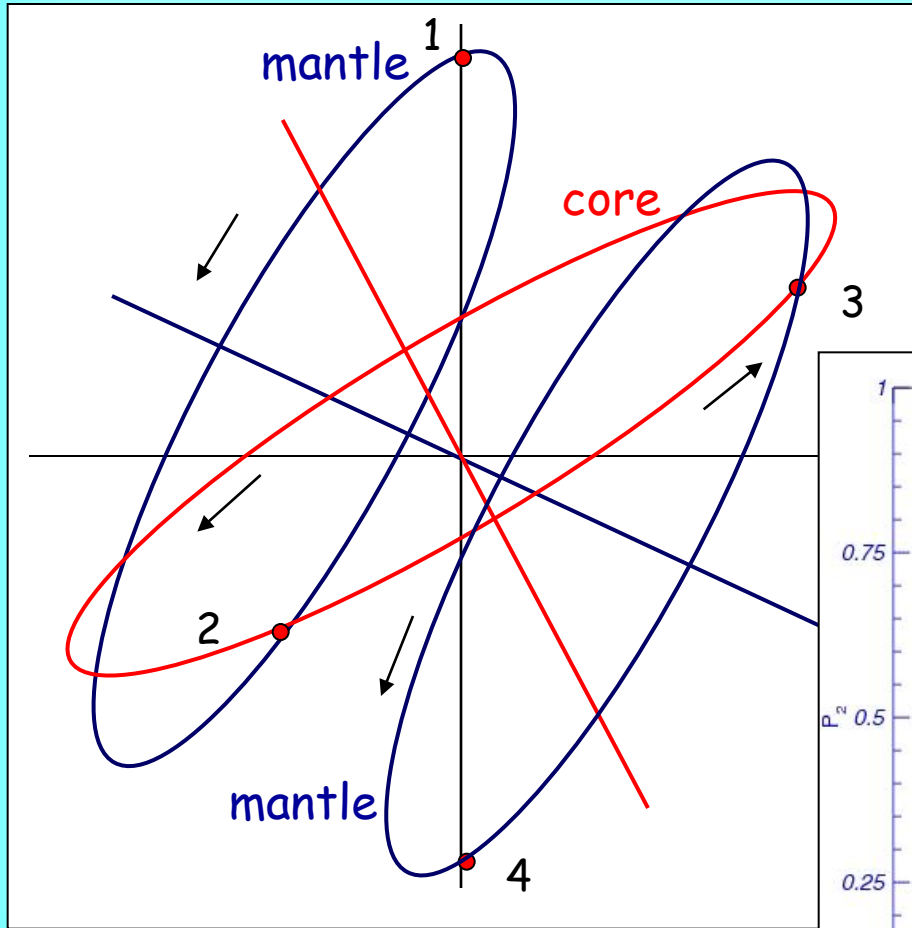
Resonance enhancement in mantle



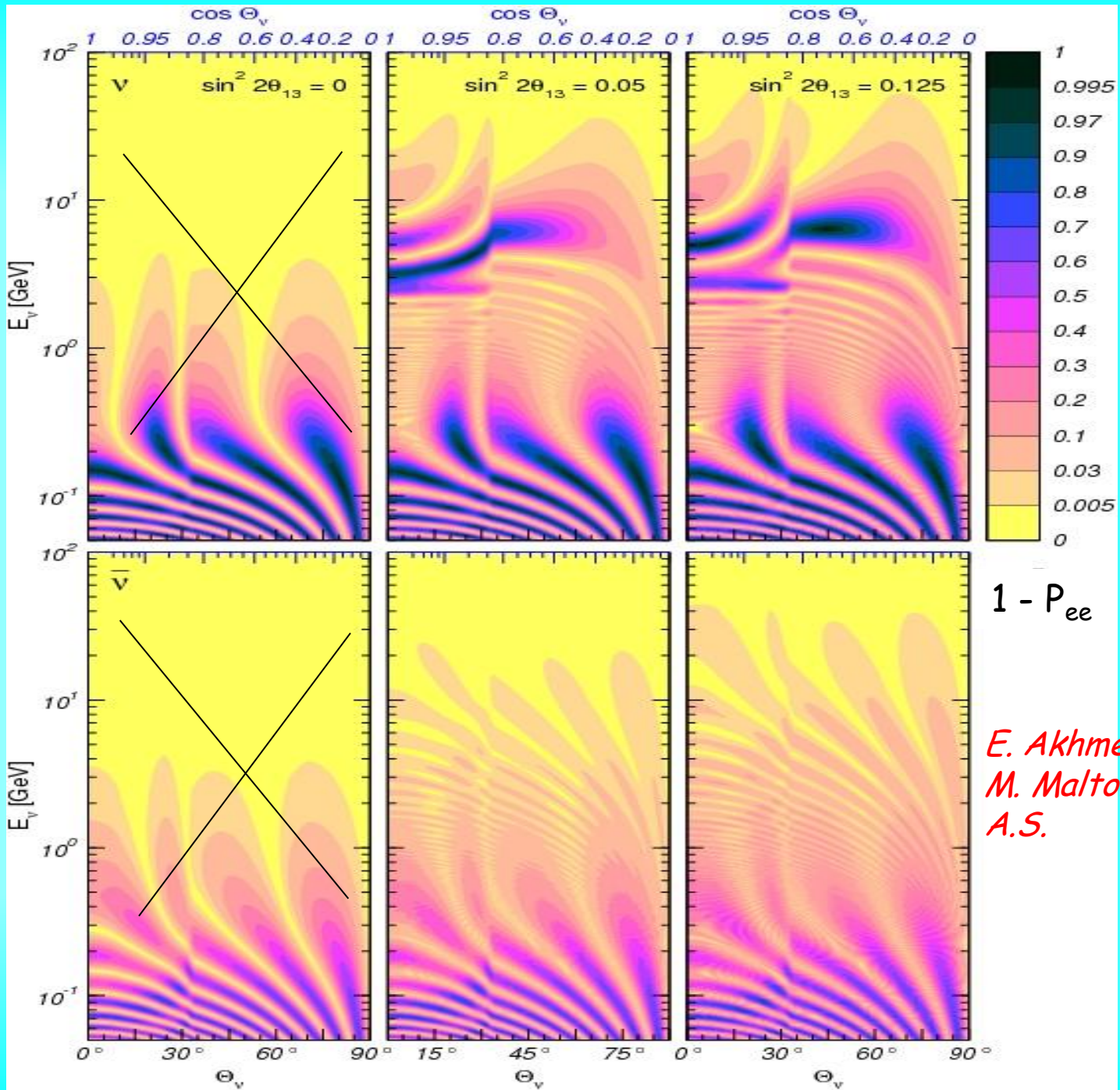
Parametric enhancement



Parametric enhancement of 1-2 mode

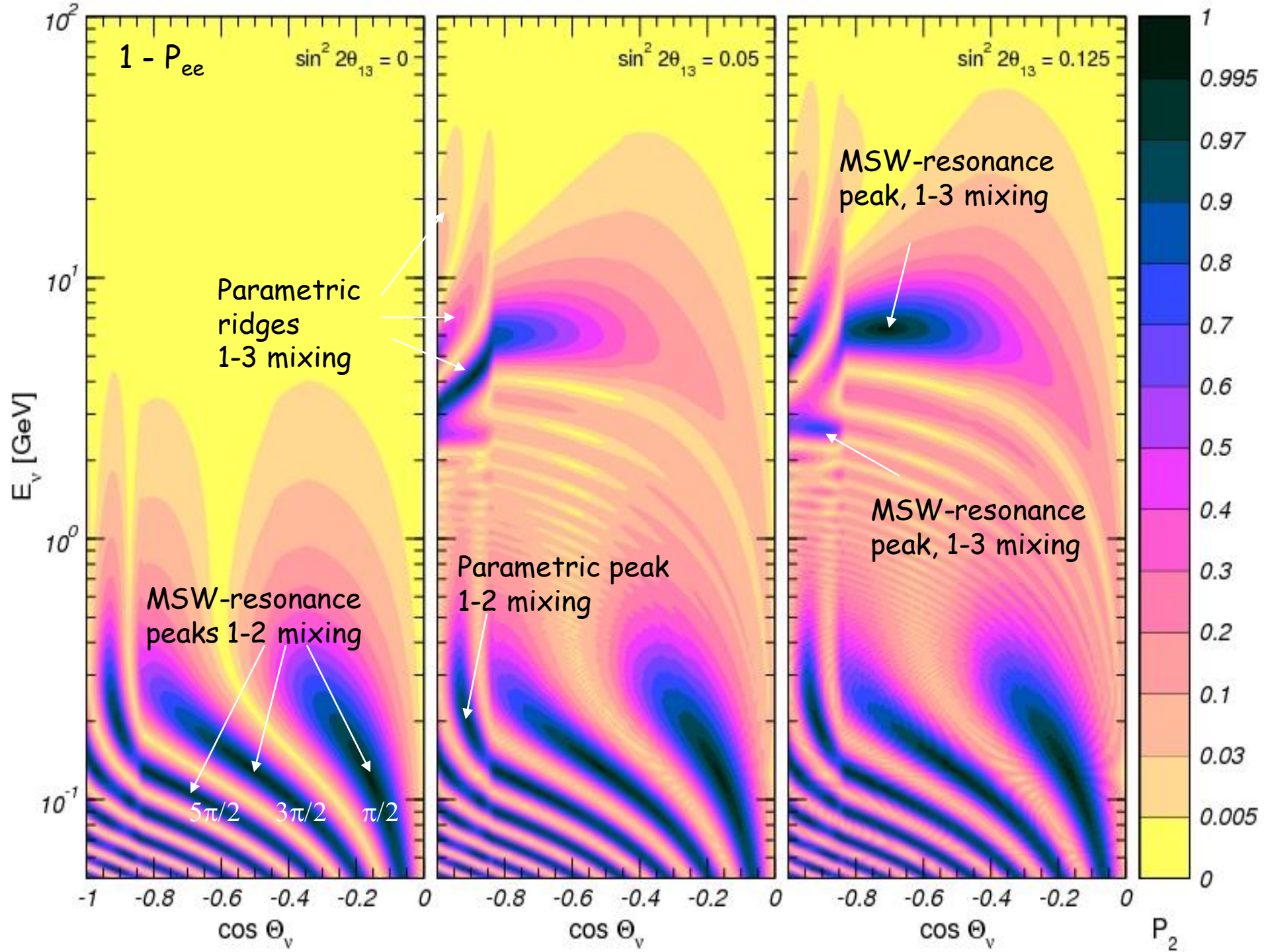


Oscillograms of the Earth



*E. Akhmedov
M. Maltoni
A.S.*

\rightleftharpoons Change of hierarchy \rightleftharpoons



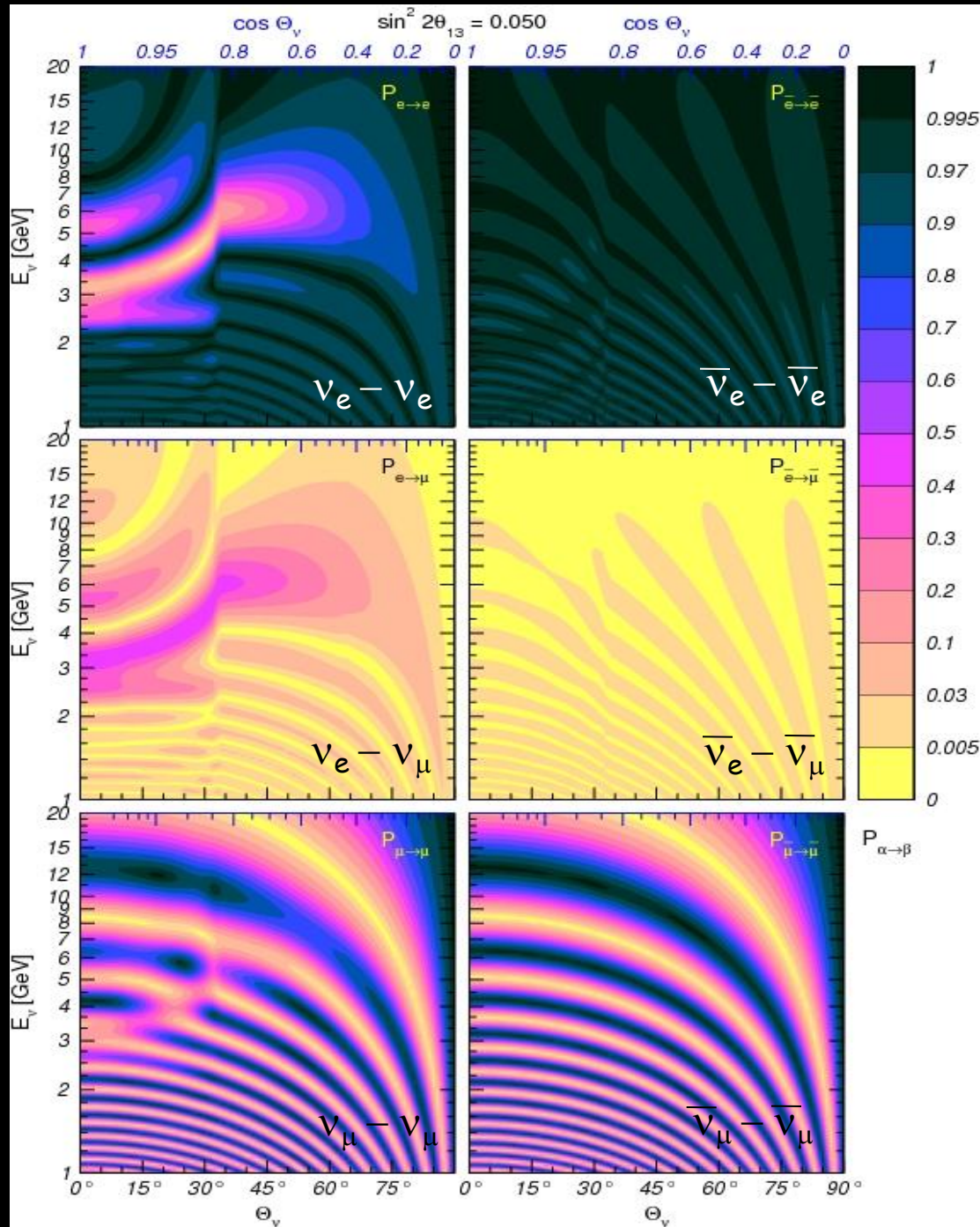
Oscillograms

$$\sin^2 2\theta_{13} = 0.050$$

Normal mass hierarchy

The Earth in neutrino light

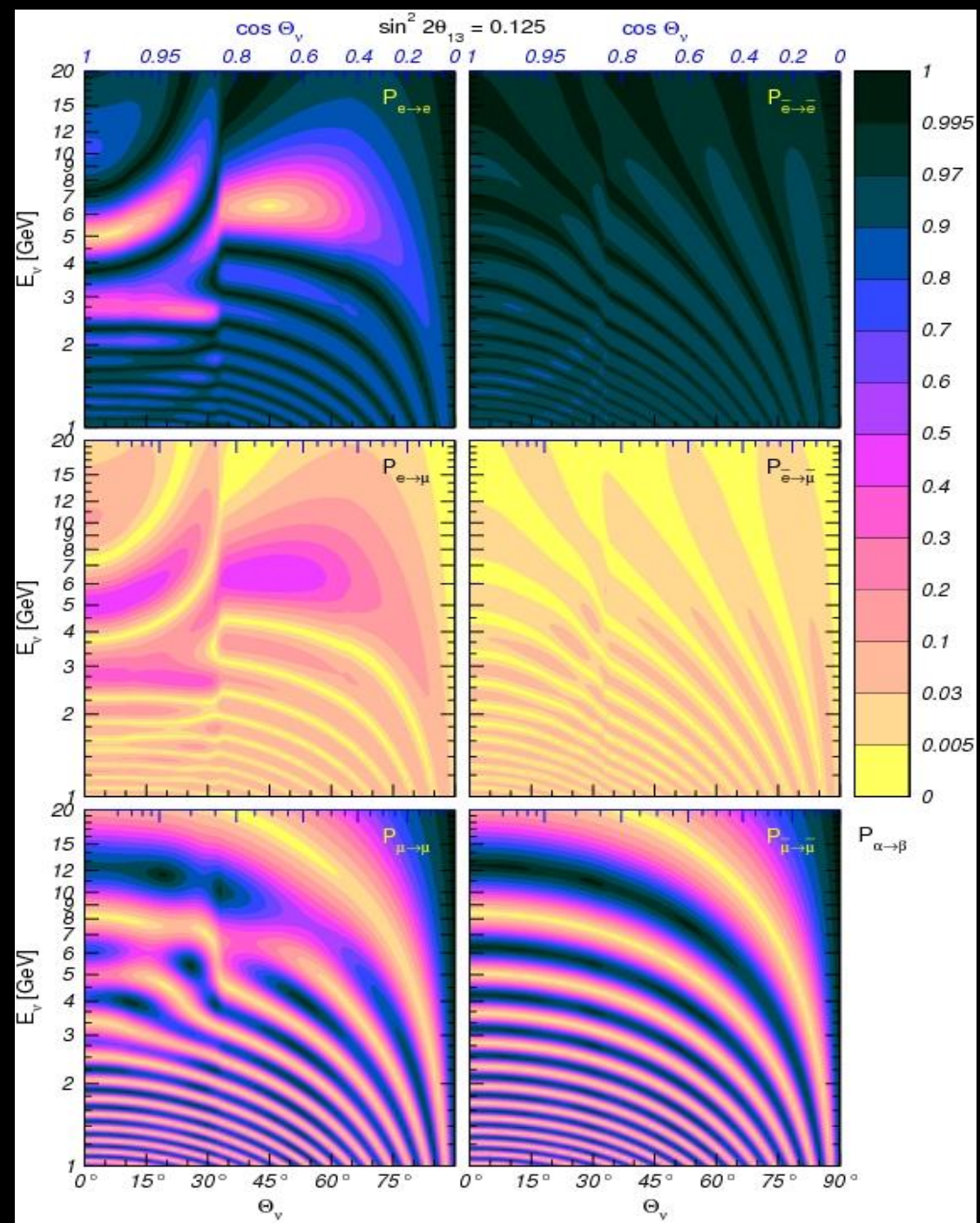
contours of constant oscillation probability in the energy- nadir (or zenith) angle plane



Oscillograms

$$\sin^2 2\theta_{13} = 0.125$$

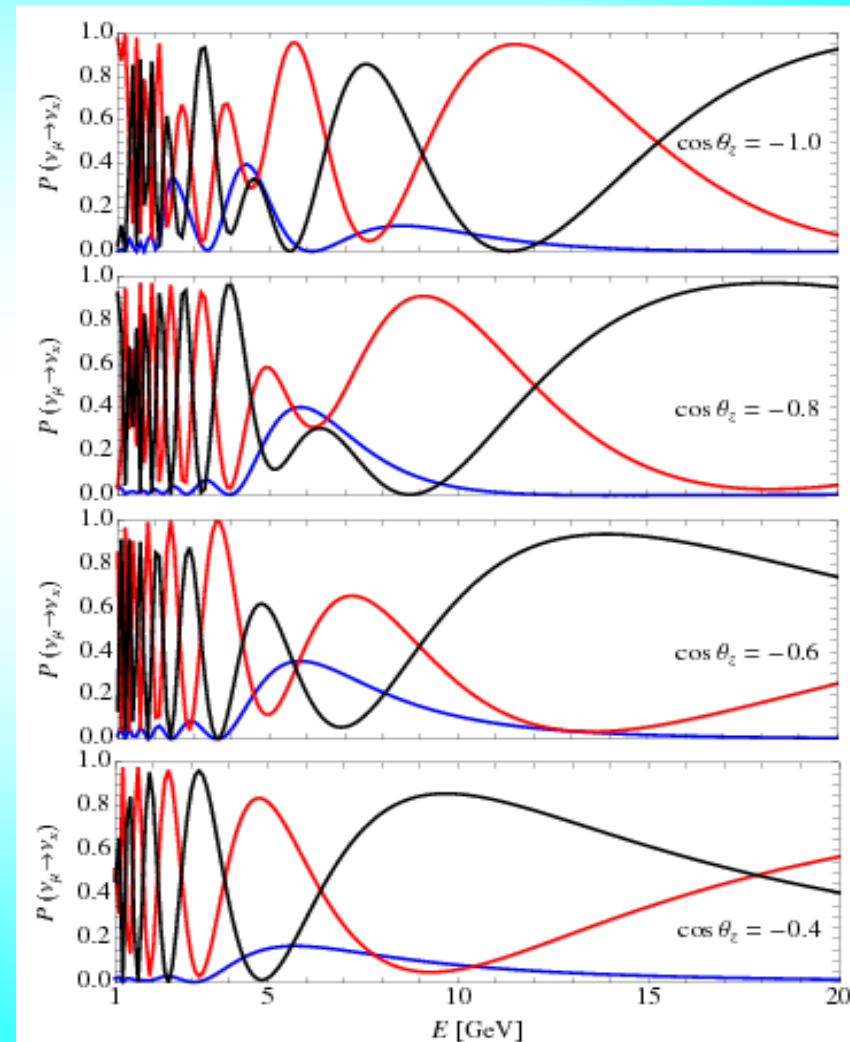
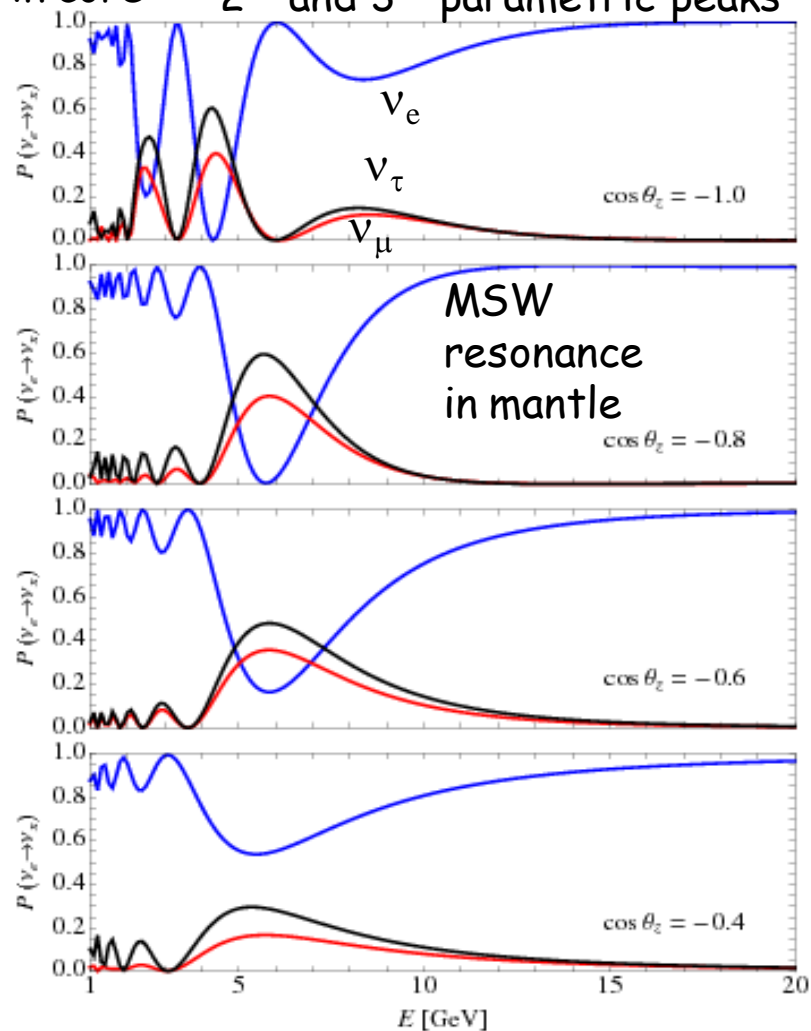
Normal mass hierarchy



Oscillation probabilities

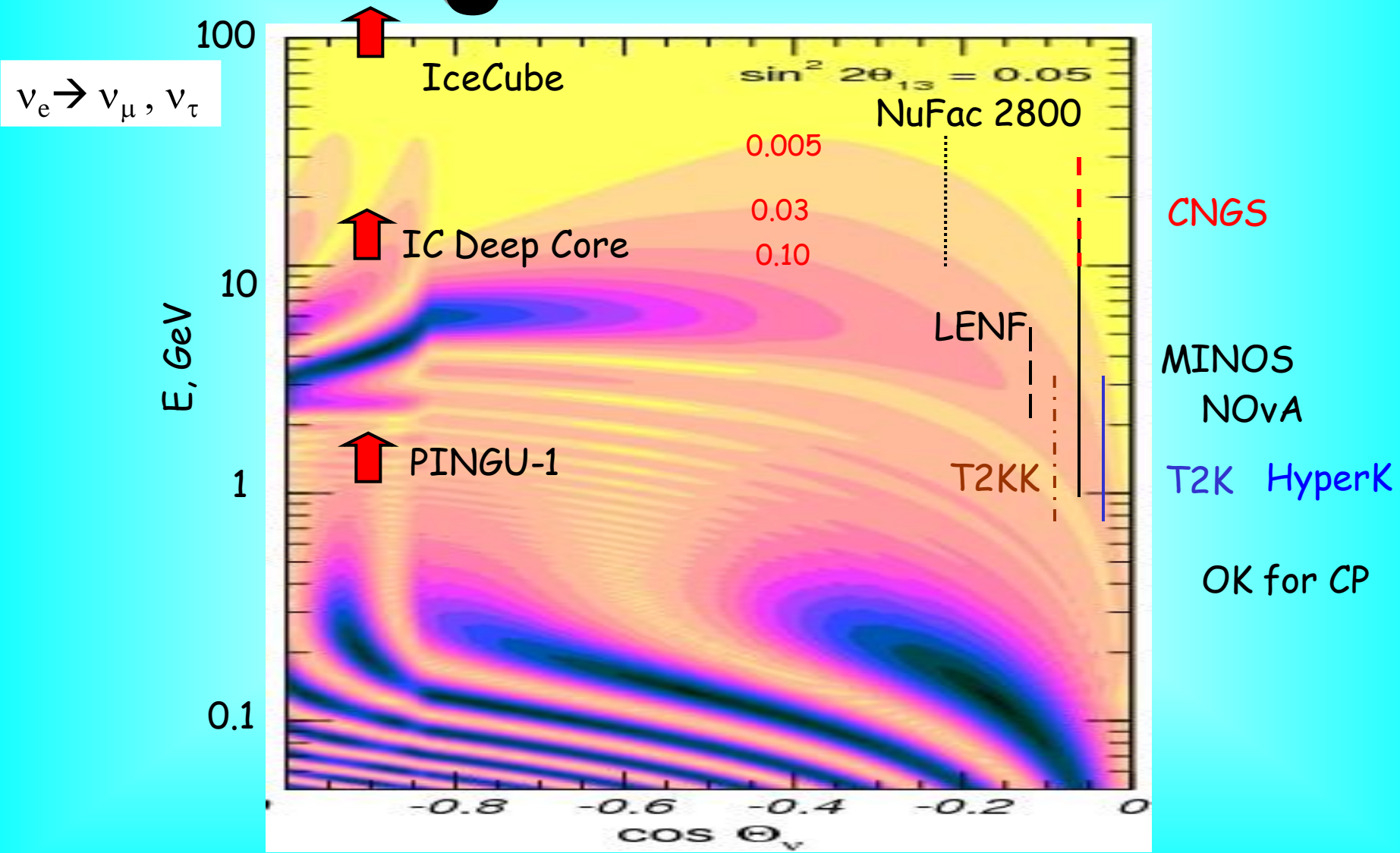
MSW
resonance
in core

2nd and 3rd parametric peaks



Oscillograms

contours of constant oscillation probability in energy- nadir (or zenith) angle plane



Atmospheric neutrinos

Oscillation physics with Huge atmospheric neutrino detectors

P. Coyle

ANTARES

Oscillations 2.7σ

DeepCore

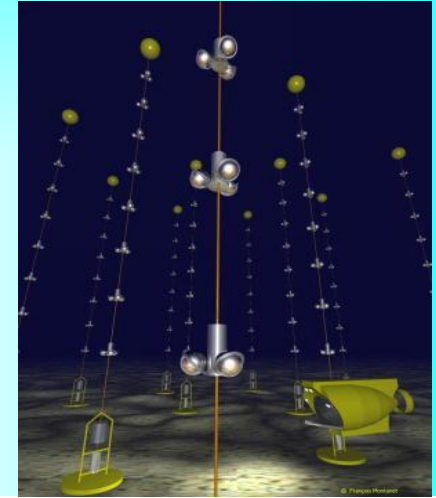
Oscillations at high energies 10 - 100 GeV in agreement with low energy data

Ice Cube

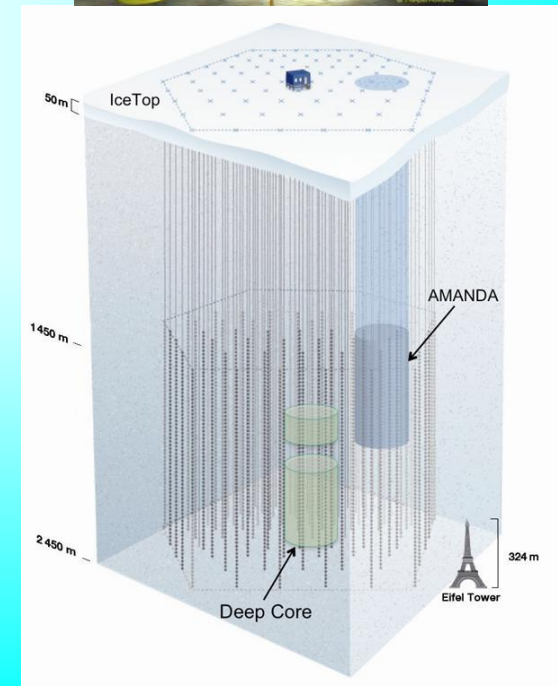
no oscillation effect at $E > 100$ GeV



Bounds on non-standard interaction, Lorentz violation etc



G. Sullivan



PINGU Geometry

Precision IceCube Next Generation Upgrade

Denser array

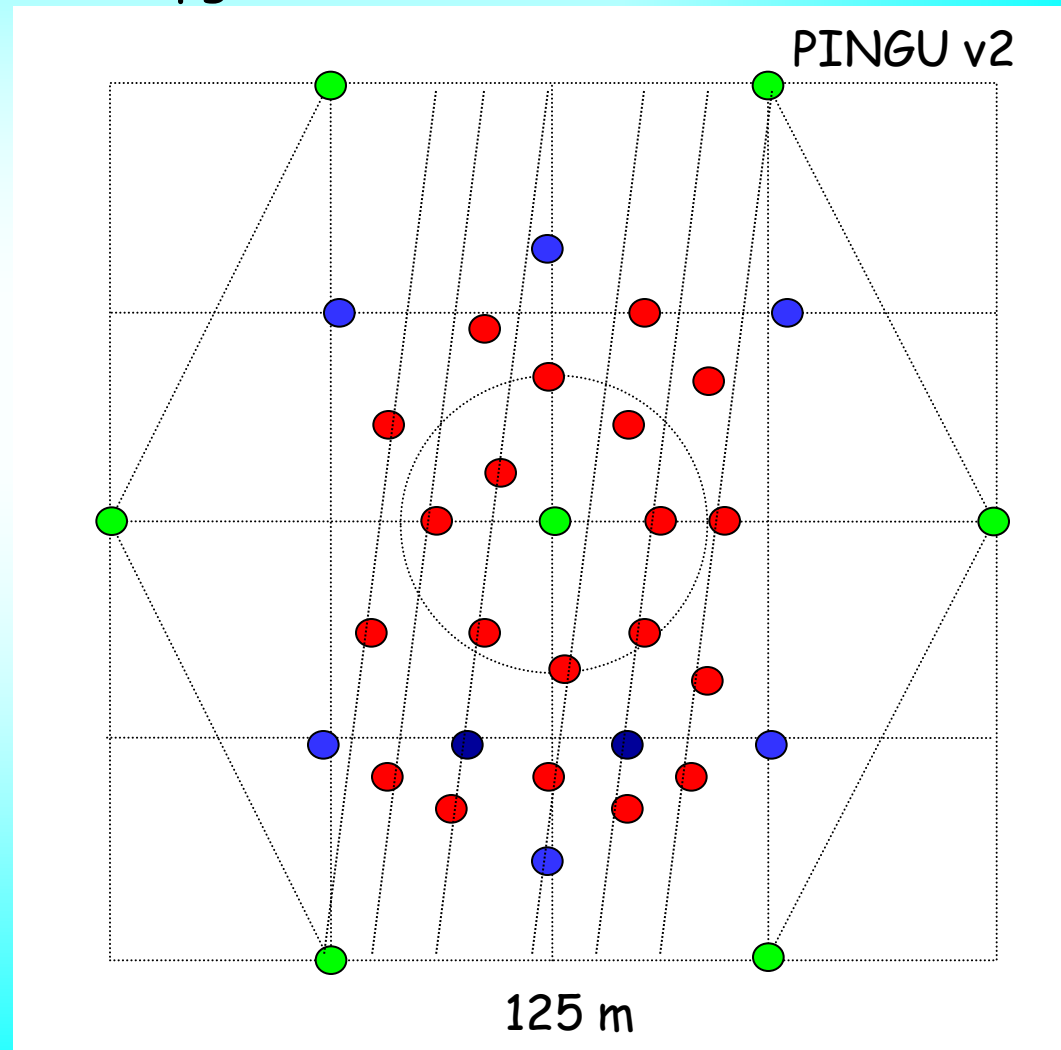
20 new strings (~60 DOMs each)
in 30 Mton DeepCore volume



Few GeV threshold in inner
10 Mton volume

Energy resolution ~ 3 GeV

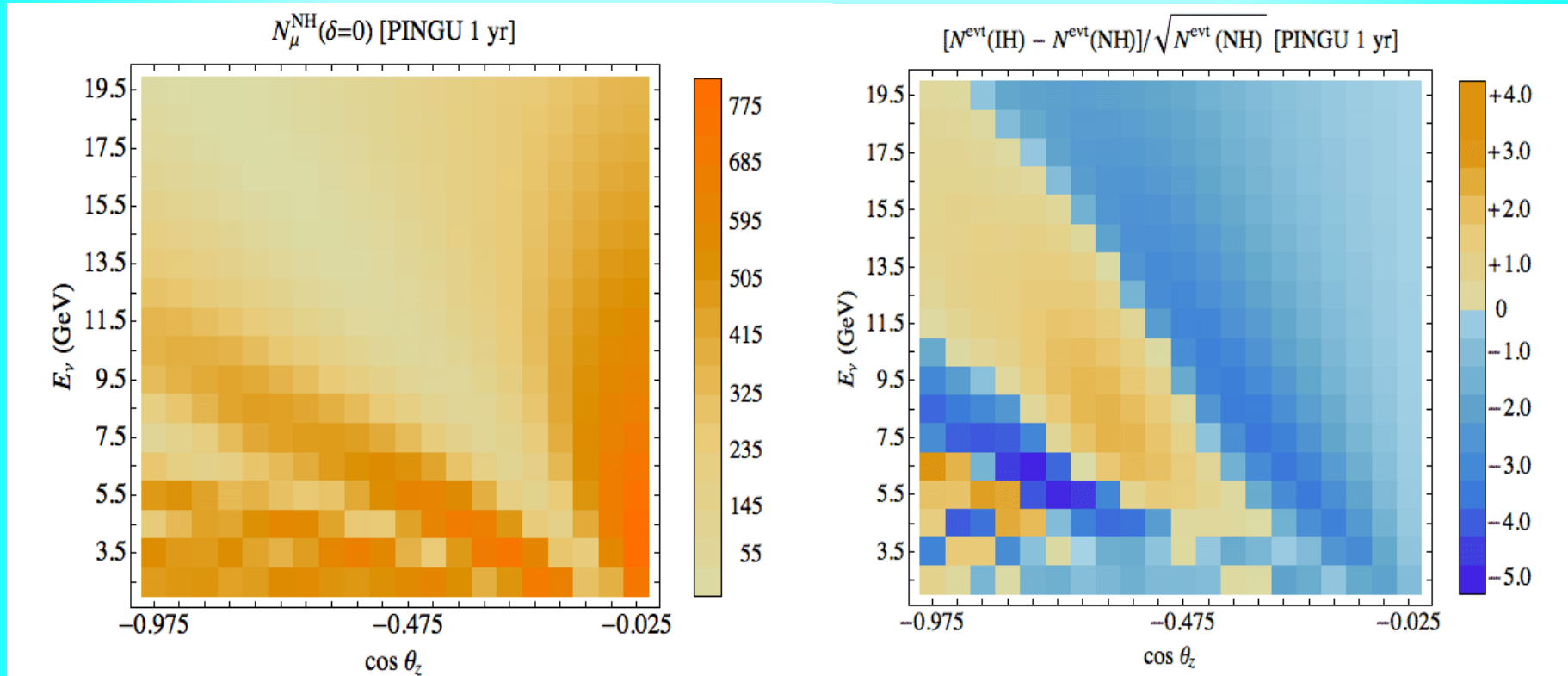
- Existing IceCube strings
- Existing DeepCore strings
- New PINGU-I strings



PINGU: Tracking events

*E. Kh Akhmedov,
S Razaque,
A. Y. S.*

Asymmetry, statistical significance



Quick estimation
of significance

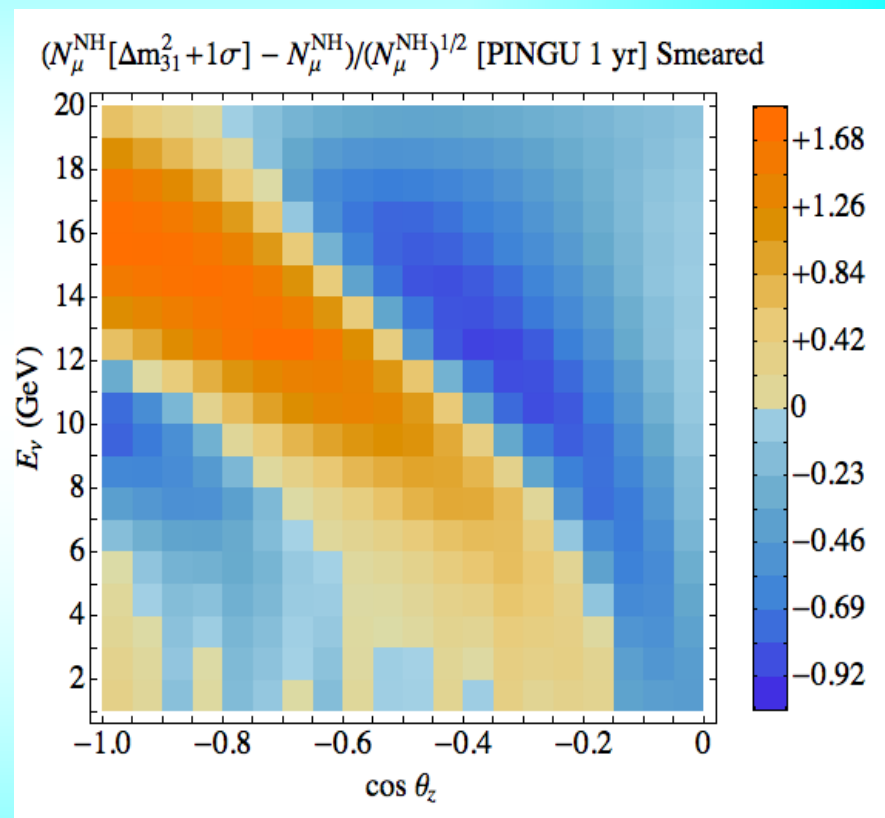
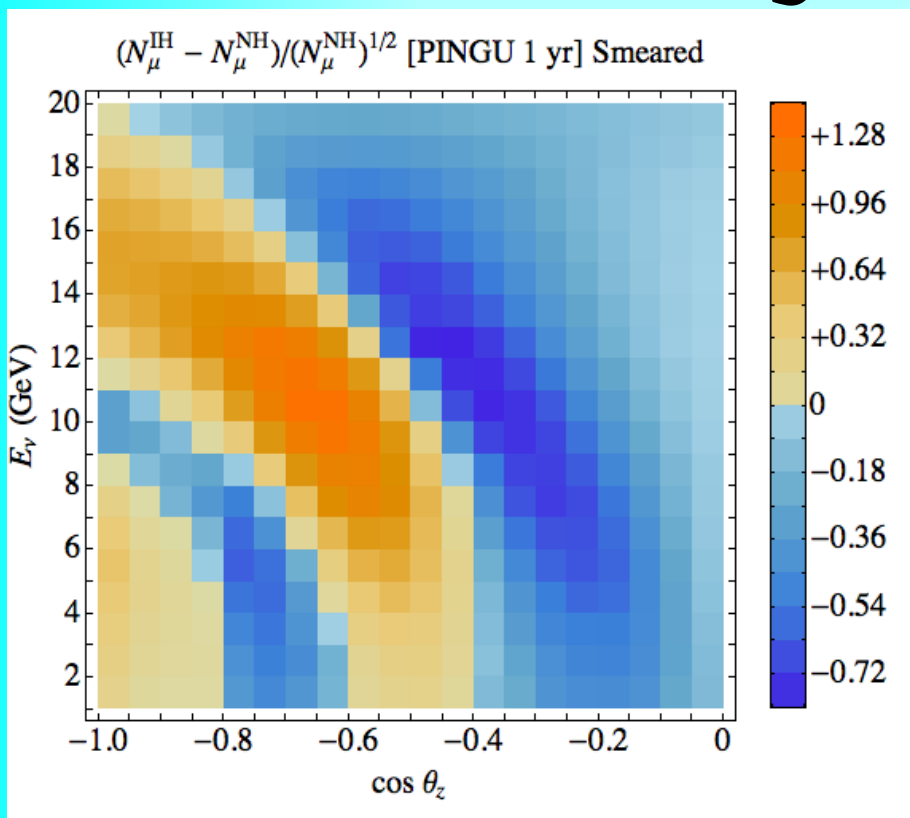
$$S_{\text{tot}} \sim s n^{1/2}$$

Effective average
significance in individual bin

Number of bins in
resolution domains

Systematics reduces
significance by factor 2

Hierarchy with PINGU



$$\sigma_E = 0.2E$$

$$\sigma_{\theta} \sim 1/E^{0.5}$$

Degeneracy

CP-violation

CP-violation

CP- transformations:

$$\nu \rightarrow \nu^c$$

$$\nu^c = i \gamma_0 \gamma_2 \nu^\dagger$$

applying to the chiral components

Under CP-transformations:

$$U_{\text{PMNS}} \rightarrow U_{\text{PMNS}}^*$$



$$\delta \rightarrow -\delta$$

$$V \rightarrow -V$$

usual medium is C -asymmetric
which leads to CP asymmetry
of interactions

Degeneracy of effects:
Matter can imitate CP-violation

Evolution

For $E > 0.1 \text{ GeV}$

Propagation basis

$$\mathbf{v}_f = \mathbf{U}_{23} \mathbf{I}_\delta \tilde{\mathbf{v}}$$

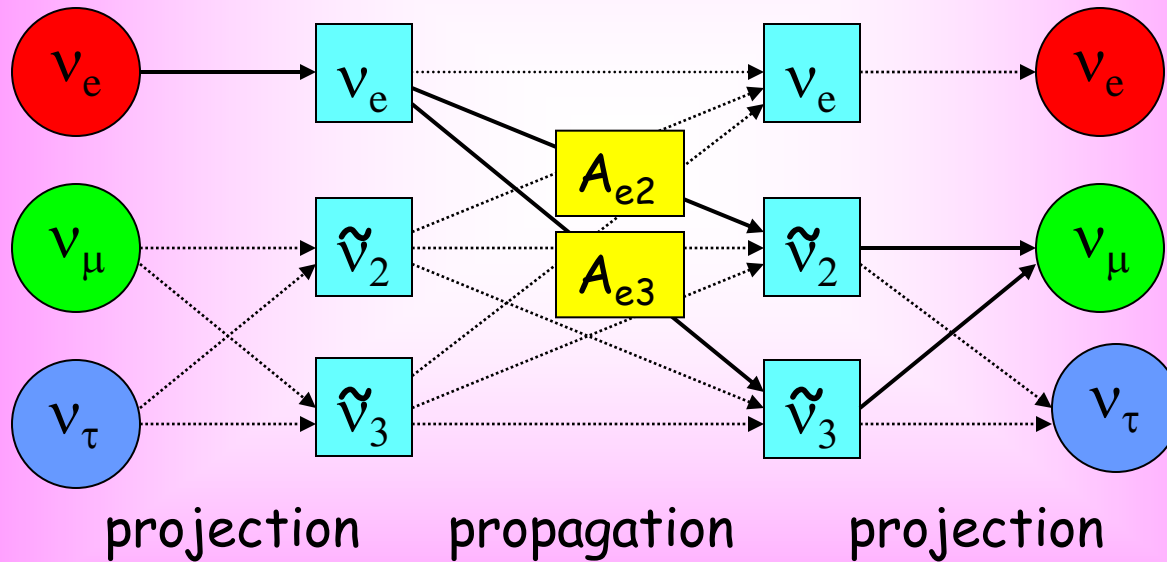


$$\mathbf{I}_\delta = \text{diag}(1, 1, e^{i\delta})$$

$$\tilde{\mathbf{H}} = \mathbf{U}_{13}^\top \mathbf{U}_{12}^\top \mathbf{H}^{\text{diag}} \mathbf{U}_{12} \mathbf{U}_{13}$$

$$\mathbf{H}^{\text{diag}} = \text{diag}(H_{1m}, H_{2m}, H_{3m})$$

CP-violation and 2-3 mixing - excluded from dynamics of propagation



projection

propagation

projection

CP appears in projection only

$$A_{22}$$

$$A_{33}$$

$$A_{23}$$

For instance:

$$A(v_e \rightarrow v_\mu) = \cos\theta_{23} A_{e2} e^{i\delta} + \sin\theta_{23} A_{e3}$$

Interference

$$P(\nu_e \rightarrow \nu_\mu) = |\cos \theta_{23} A_{e2} e^{i\delta} + \sin \theta_{23} A_{e3}|^2$$

“solar” amplitude

“atmospheric” amplitude

dependence on
 δ and θ_{23} is explicit

“Factorization”
approximation:

A_{e2} depends mainly on $\Delta m_{12}^2, \theta_{12}$

A_{e3} depends mainly on $\Delta m_{13}^2, \theta_{13}$

corrections of the order $\Delta m_{12}^2 / \Delta m_{13}^2, s_{13}^2$

For constant density:

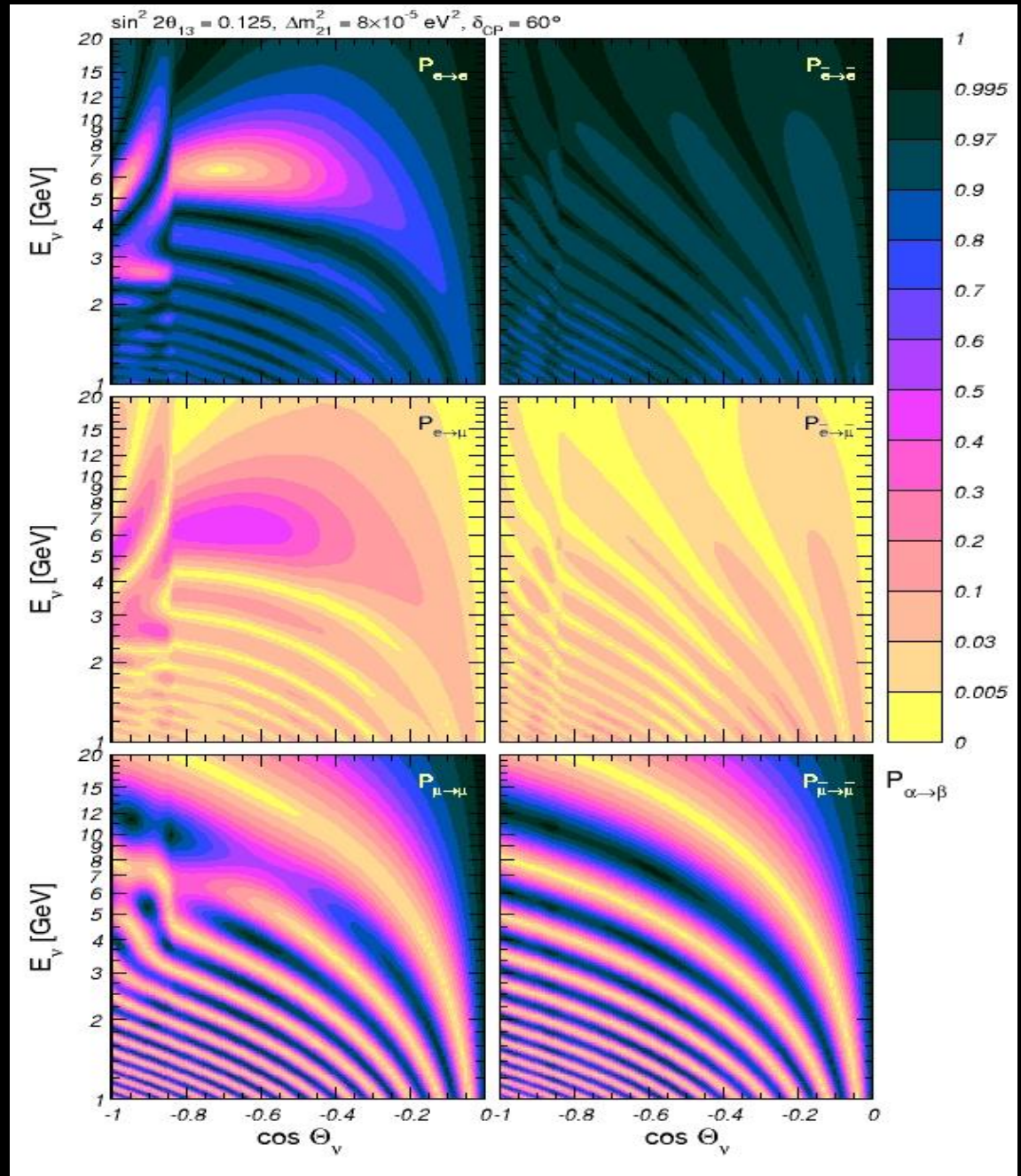
$$A_{e2} \sim i \sin 2\theta_{12}^m \sin \frac{\pi L}{l_{12}^m}$$
$$A_{e3} \sim i \sin 2\theta_{13}^m \sin \frac{\pi L}{l_{13}^m}$$

up to phase
factors

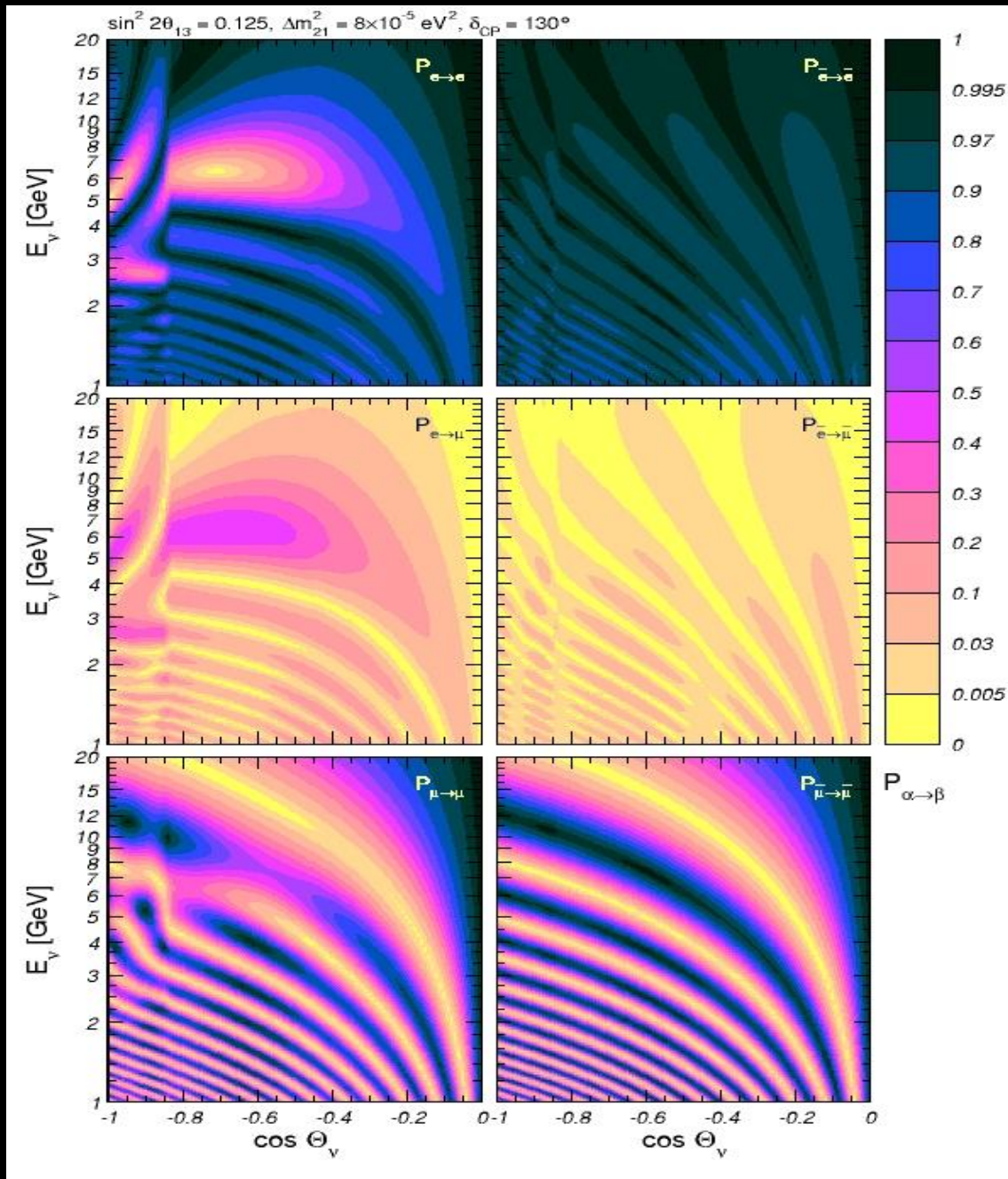
CP-violation

$$\delta = 60^\circ$$

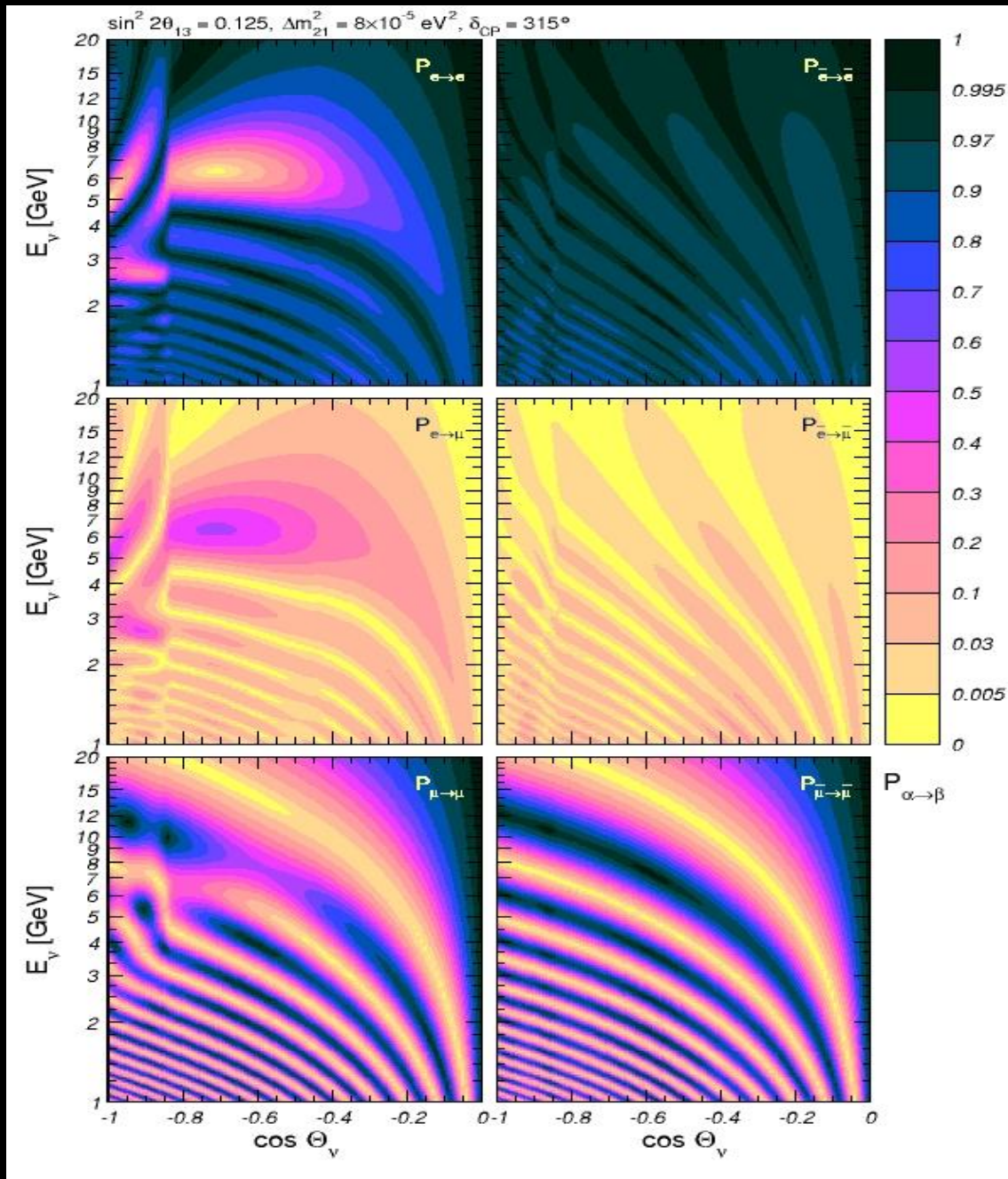
Standard
parameterization



$$\delta = 130^\circ$$



$$\delta = 315^\circ$$



CP-violation domains

Three grids
of lines:

Solar magic lines

Atmospheric magic lines

Interference phase lines

"Magic lines"

P. Huber, W. Winter
V. Barger, D. Marfatia,
K Whisnant, A.S.

Explicitly

$$P(\nu_e \rightarrow \nu_\mu) = c_{23}^2 |A_{e2}|^2 + s_{23}^2 |A_{e3}|^2 + 2s_{23}c_{23} |A_{e2}| |A_{e3}| \cos(\phi + \delta)$$

$$\phi = \arg(A_{e2} A_{e3}^*)$$

$$P_{\text{int}} = 2s_{23}c_{23} |A_{e2}| |A_{e3}| \cos(\phi + \delta)$$

Dependence on δ disappears, interference term is zero if

$$P_{\text{int}} = 0$$



$$A_{e2} = 0 \quad \text{- solar magic lines}$$



$$A_{e3} = 0 \quad \text{- atmospheric magic lines}$$



$$(\phi + \delta) = \pi/2 + 2\pi k \quad \text{- interference phase condition}$$



$$\phi(E, L) = -\delta + \pi/2 + \pi k$$

depends on δ

"Magic lines"

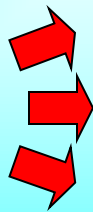
For $\nu_\mu \rightarrow \nu_\mu$ channel

$$P_{\text{int}} \sim 2s_{23}c_{23}|A_{e2}||A_{e3}|\cos\phi \cos\delta$$

- The survival probabilities is CP-even functions of δ
- no CP-violation
- dependences on phases factorize

Dependence on δ disappears

$$P_{\text{int}} = 0$$



$$A_{e2} = 0$$

$$A_{e3} = 0$$

$$\phi = \pi/2 + \pi k$$

interference phase
does not depends on δ

Form the phase line grid

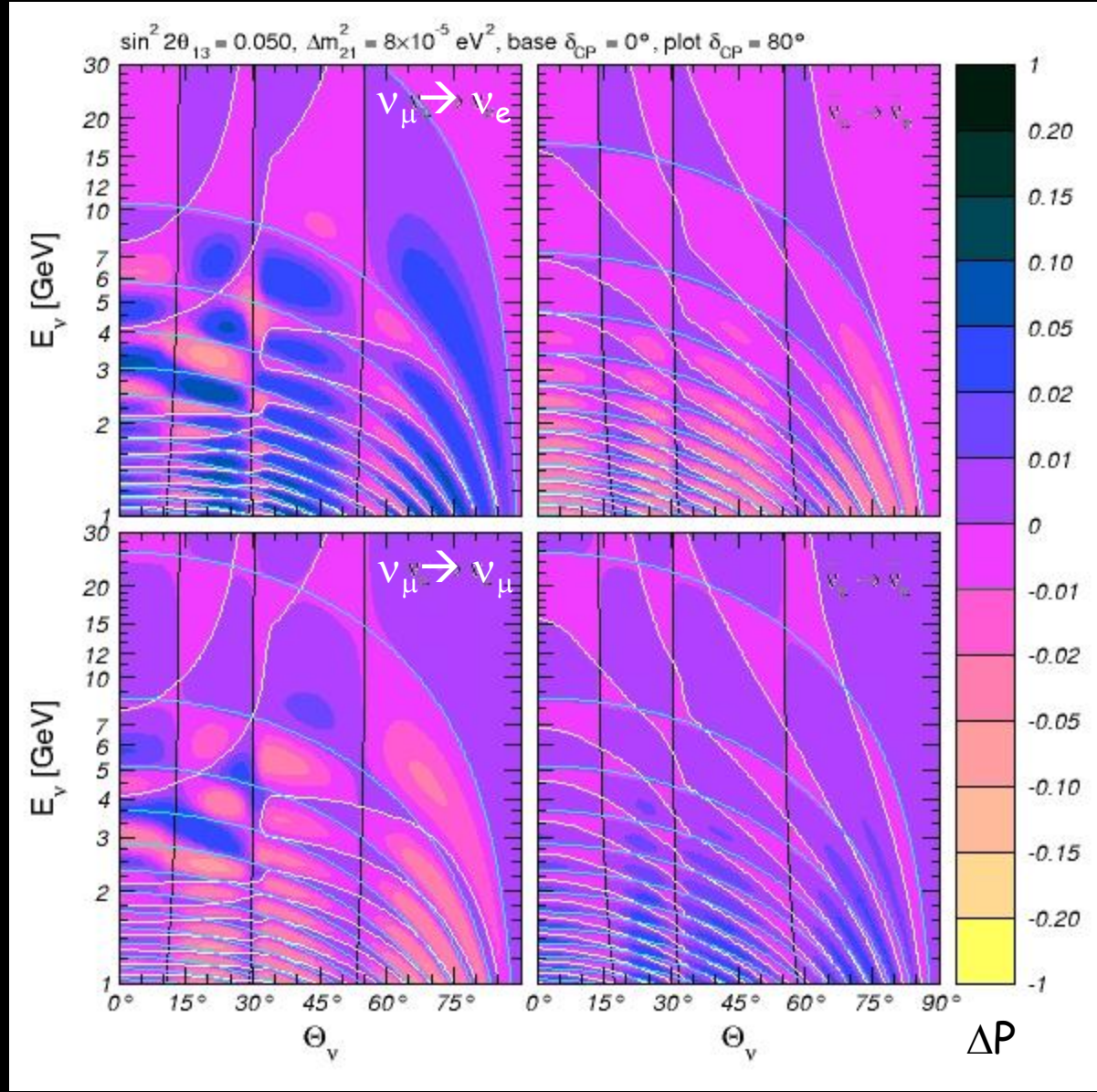
$$\Delta P = P(\delta) - P(\delta_f) = \text{const}$$

Int. phase line (blue) moves with δ -change

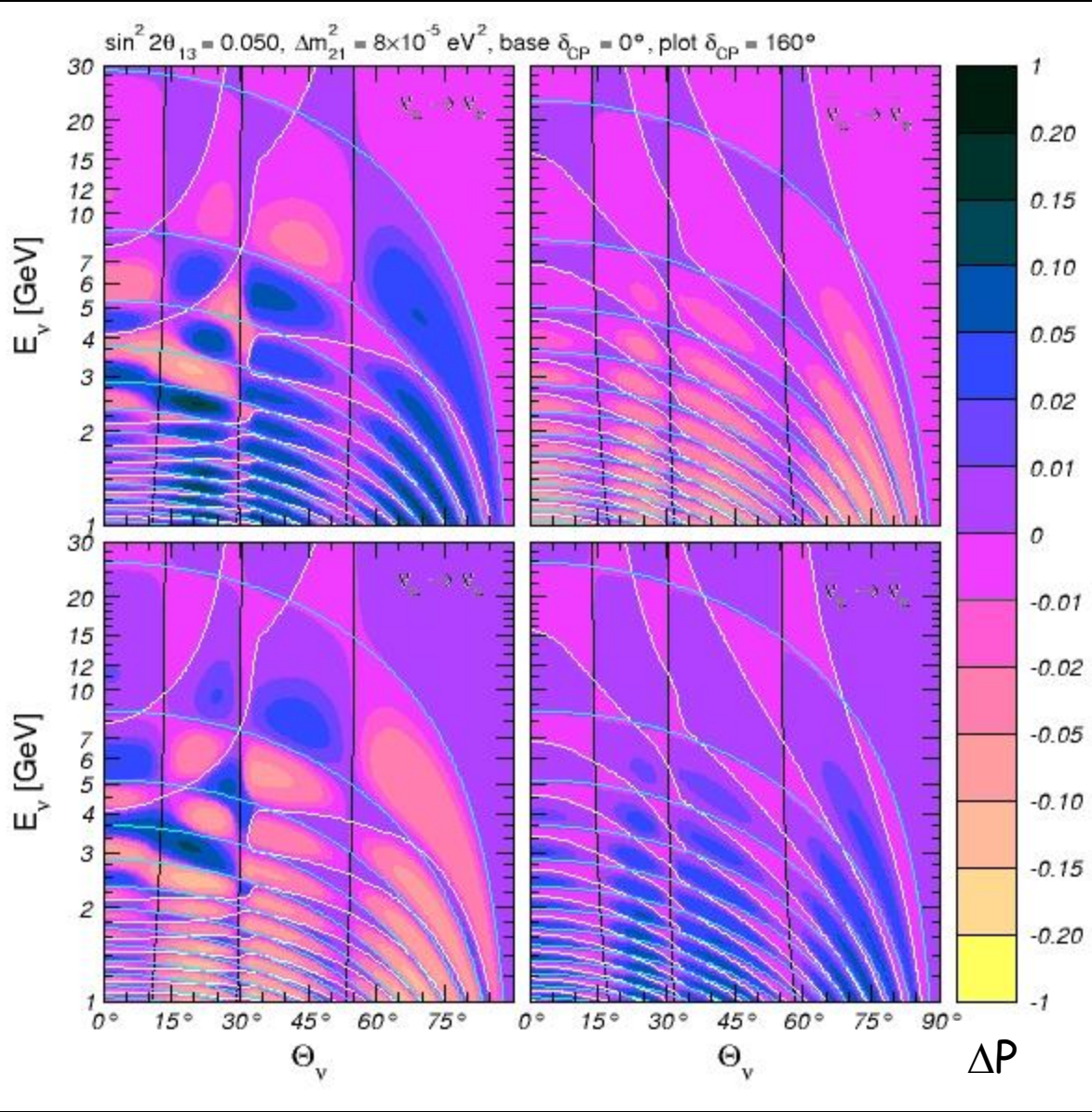


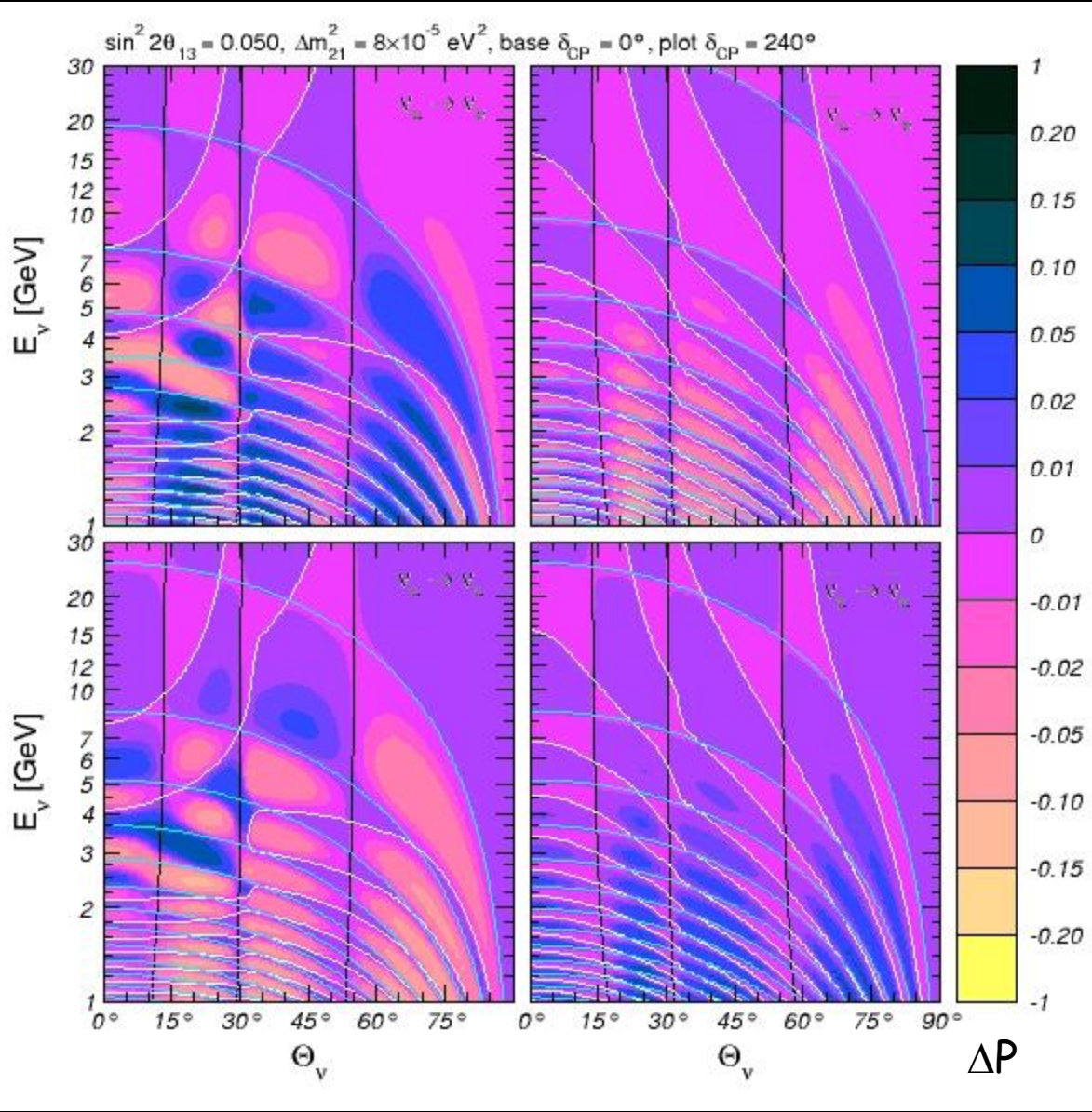
Grids do not change with δ

Black: solar
White: atmospheric

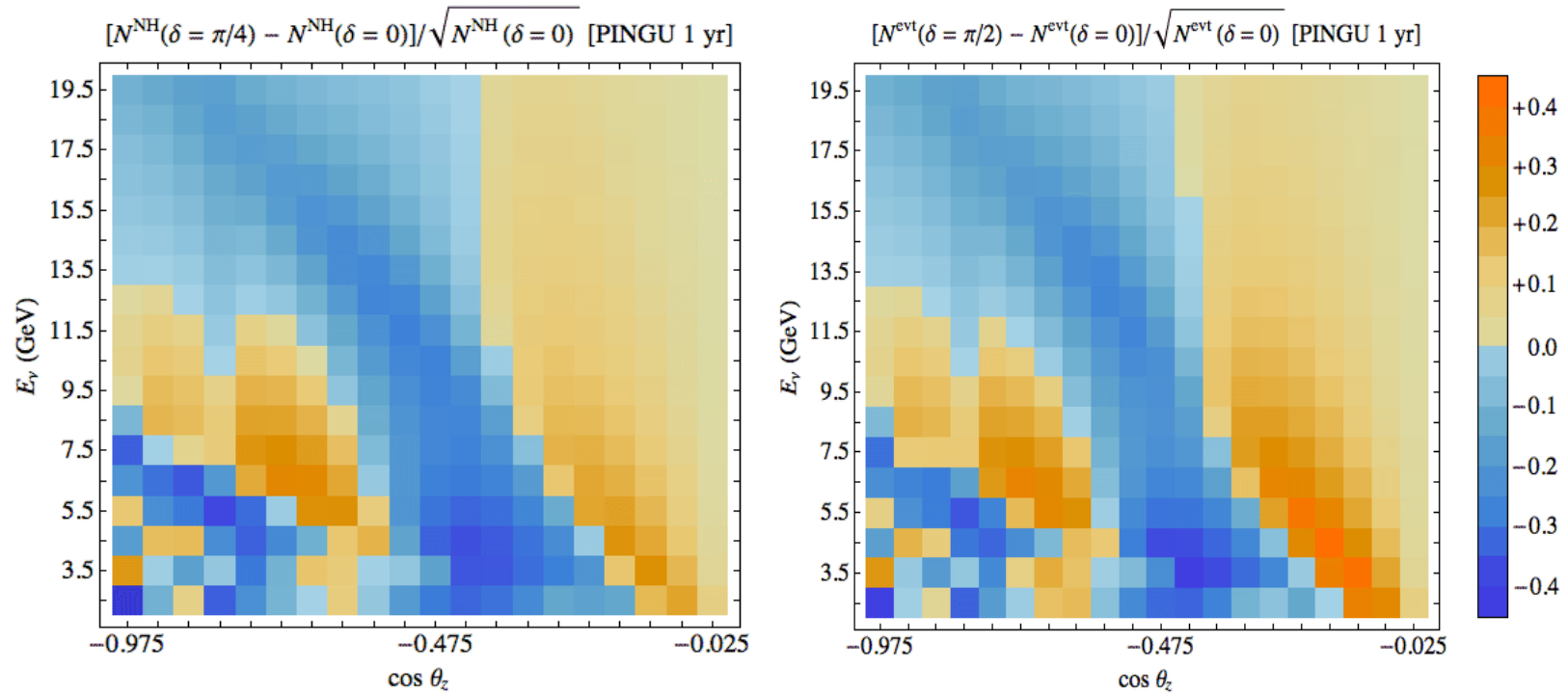


Magic grid





CP asymmetry



Summary

All three mixing angles are measured

Determination of 1-3 mixing (which turns out to be not very small)
→ strong impact on phenomenology, theory and future experimental programs

Indications of significant deviation of the 2-3 mixing from maximal
→ important implications for theory

Next step: determination of neutrino mass hierarchy and CP-violating phase

Studies of atmospheric neutrinos with huge (multi-megaton scale detectors) can play crucial role

Establishing the absolute neutrino mass scale, and Majorana nature → among main goals